

Communication Basics

Serialization, Bit Synchronization, Physical Aspects of Transmission,
Transmission Frame, Frame Synchronization, Error Control

Agenda

- **Introduction**
- **Bit Synchronization**
 - Asynchronous
 - Synchronous
- **Physical Aspects**
 - Mathematical Background
 - Communication Channel / Modulation
 - Serialization / Propagation Delay
- **Transmission Frame**
 - Generic Format
 - Frame Synchronization
 - Error Control

Information

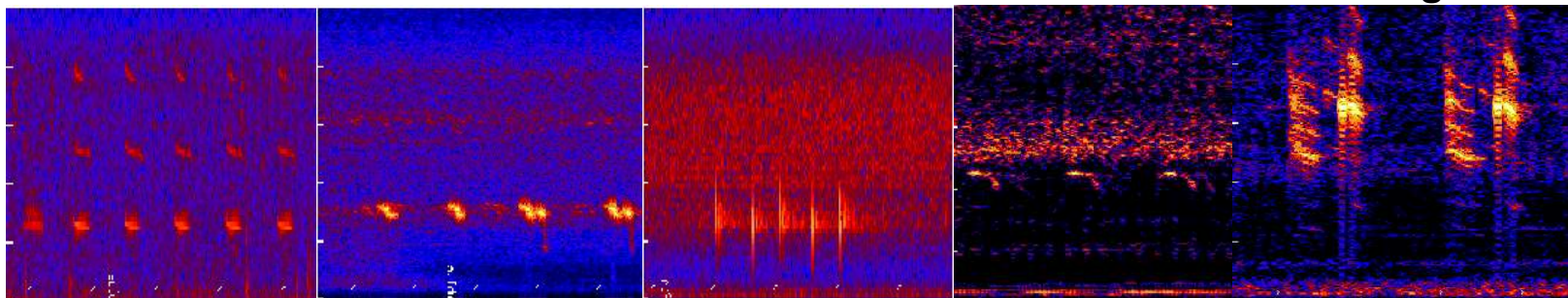
- ***What is information?***
 - Represented and carried by **symbols**
 - **Recognized** by receiver (hopefully)
 - *Interpretation* is the key...



Symbols

- **Symbols (may) represent information**
 - Voice patterns (Speech)
 - Sign language, Pictograms 🌐 🧑 🗣️ 📺
 - Scripture
 - Voltage and current levels
 - Light pulses

Blue Whale Sonograms



Representation of Symbols for Information Processing, Storage and Exchange

- In the context of computer systems and data communication
- Discrete levels = "Digital"
 - Resistant against noise
- How many levels?
 - Binary (easiest)
 - Bit (binary digit), values 0 and 1
 - M-ary: *More information per time unit!*

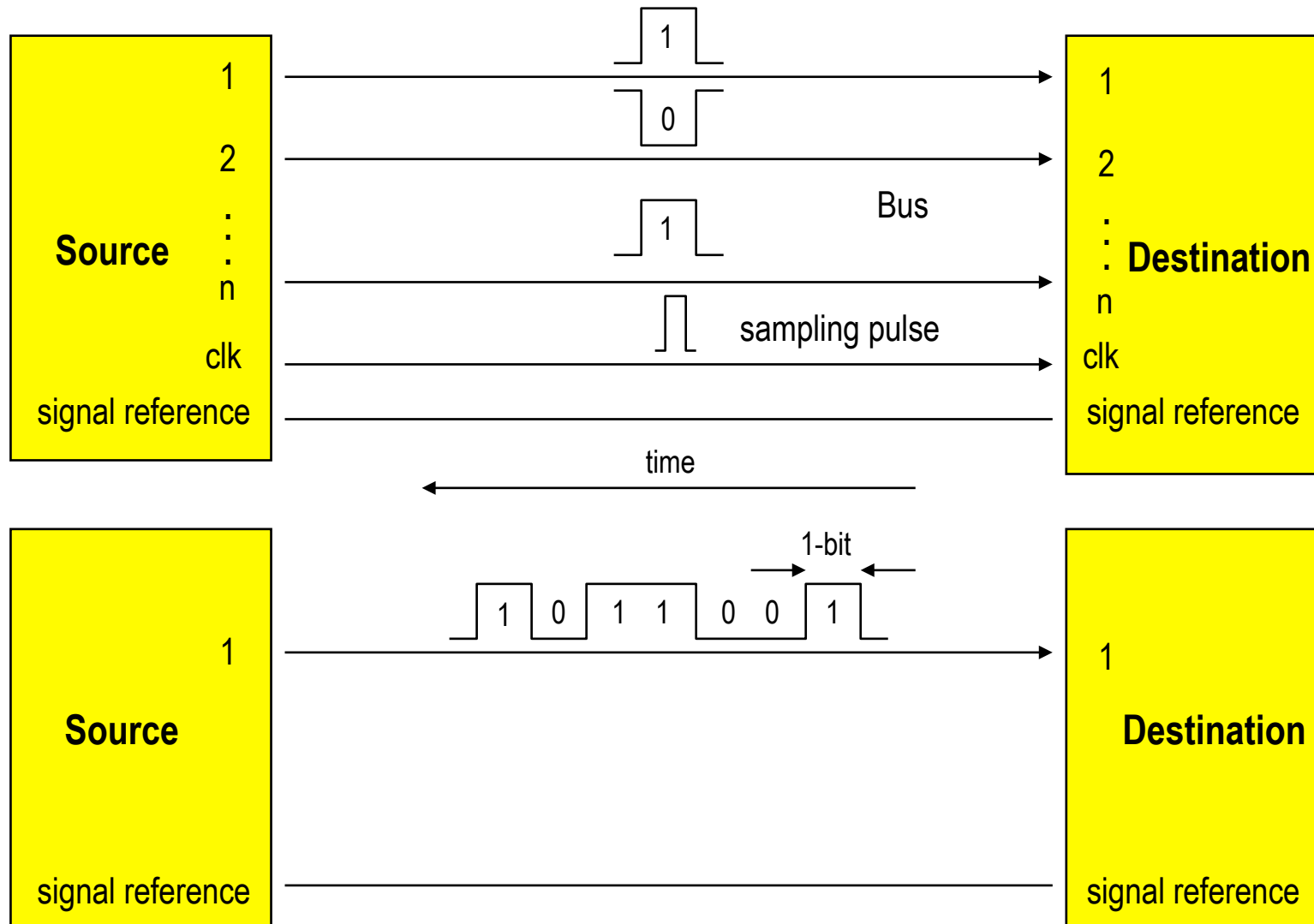


Binary

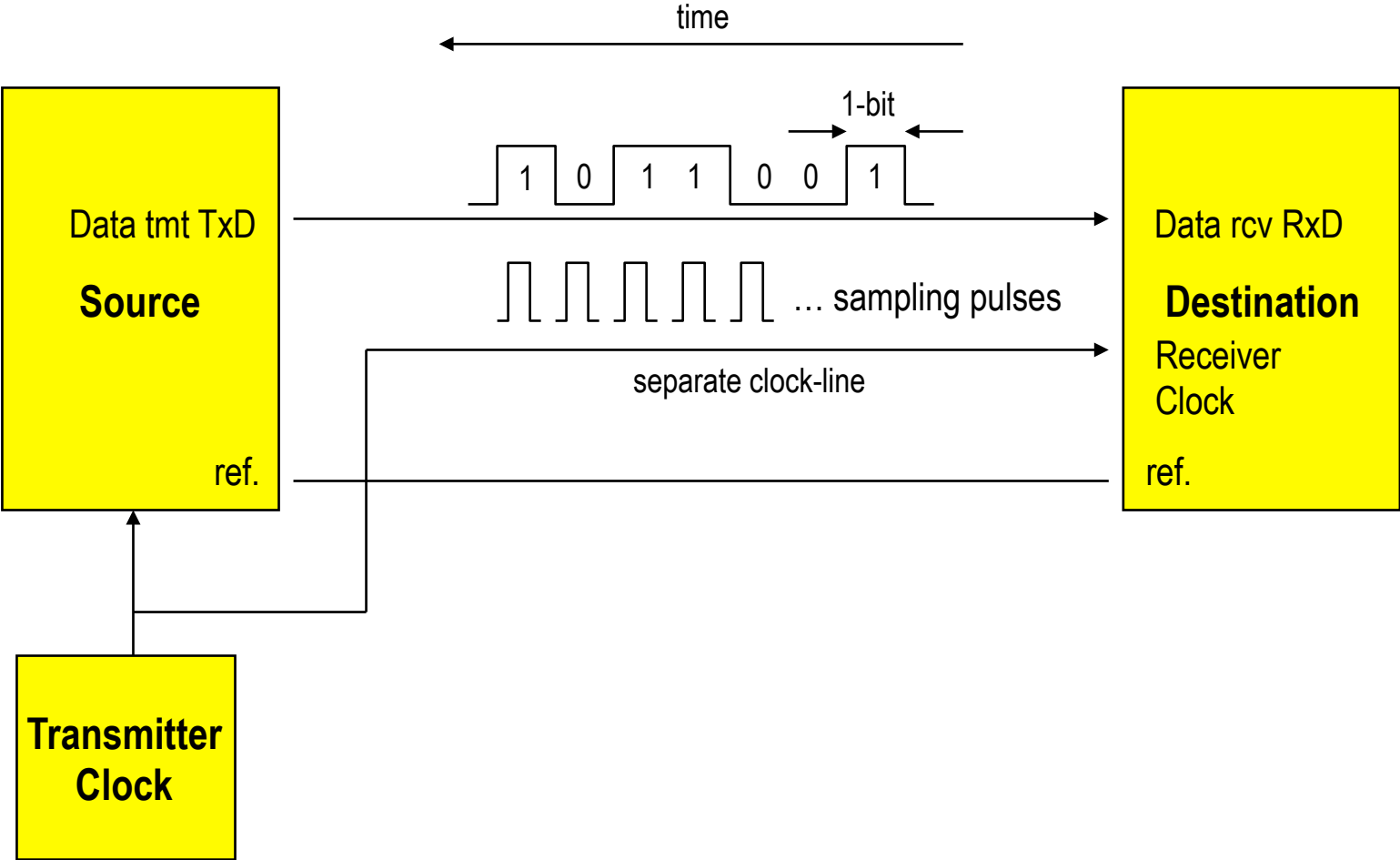


M-ary
(here 4 levels, e. g. ISDN)

Transmission of Information: Parallel versus Serial



Separate Clock-Line ?

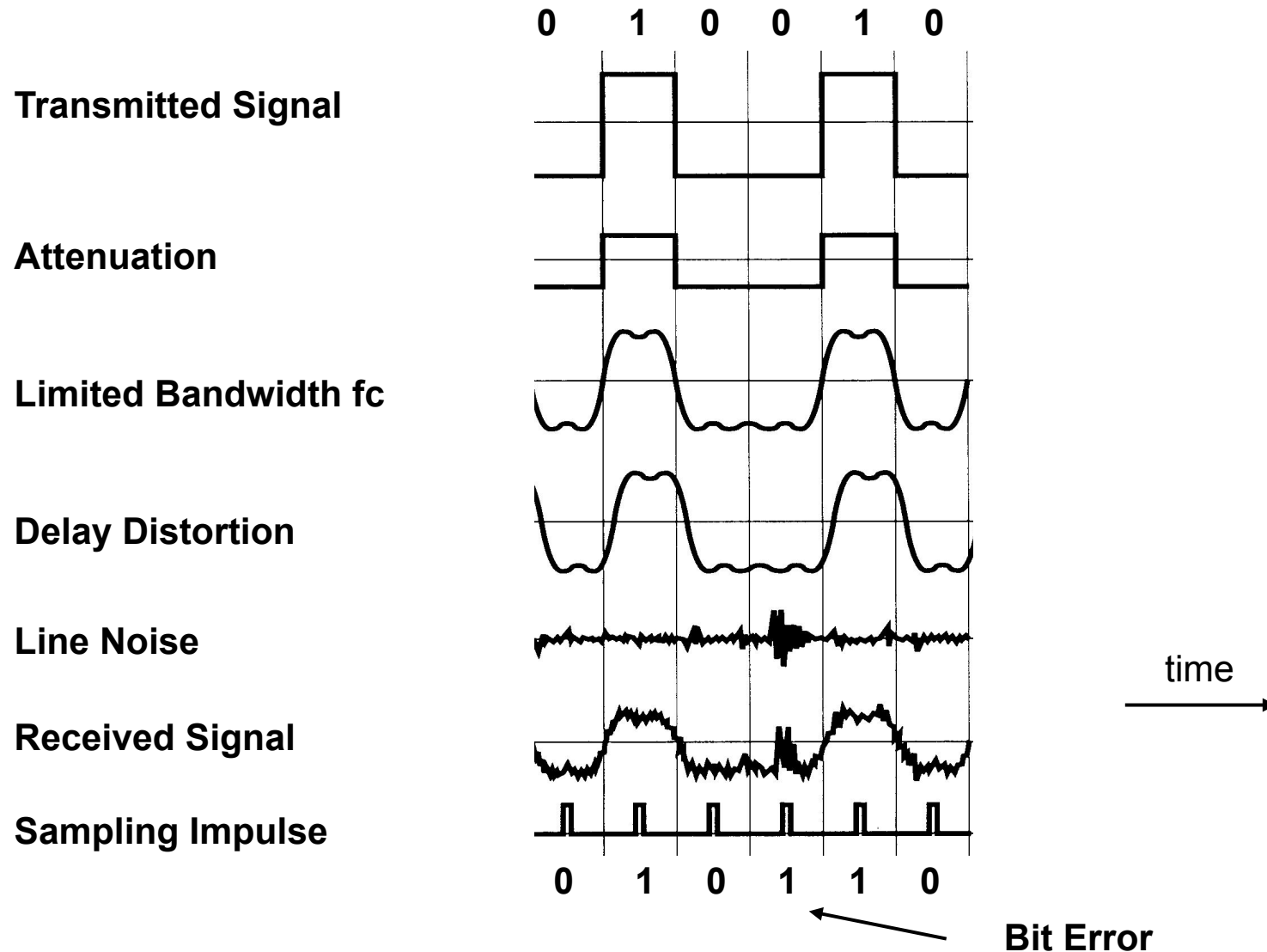


Parallel versus Serial

- **Parallel transmission**
 - Multiple data wires (fast)
 - **Explicit clocking wire**
 - Simple synchronization but not cost-effective
 - Only useful for small distances

- **Serial transmission**
 - Only one wire (-pair)
 - **No clocking wire**
 - **Most important** for data communication for long distances
 - Bit (clock) synchronization is necessary

What Happens To A Signal On The Wire?

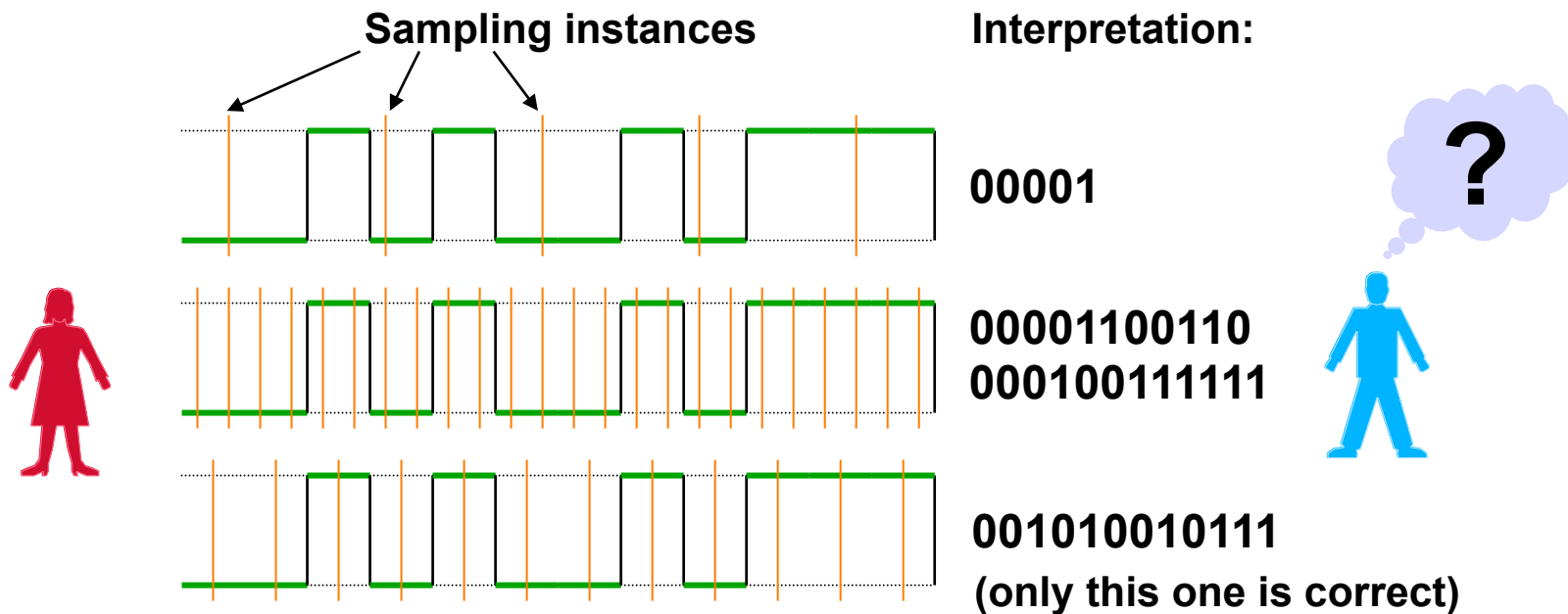


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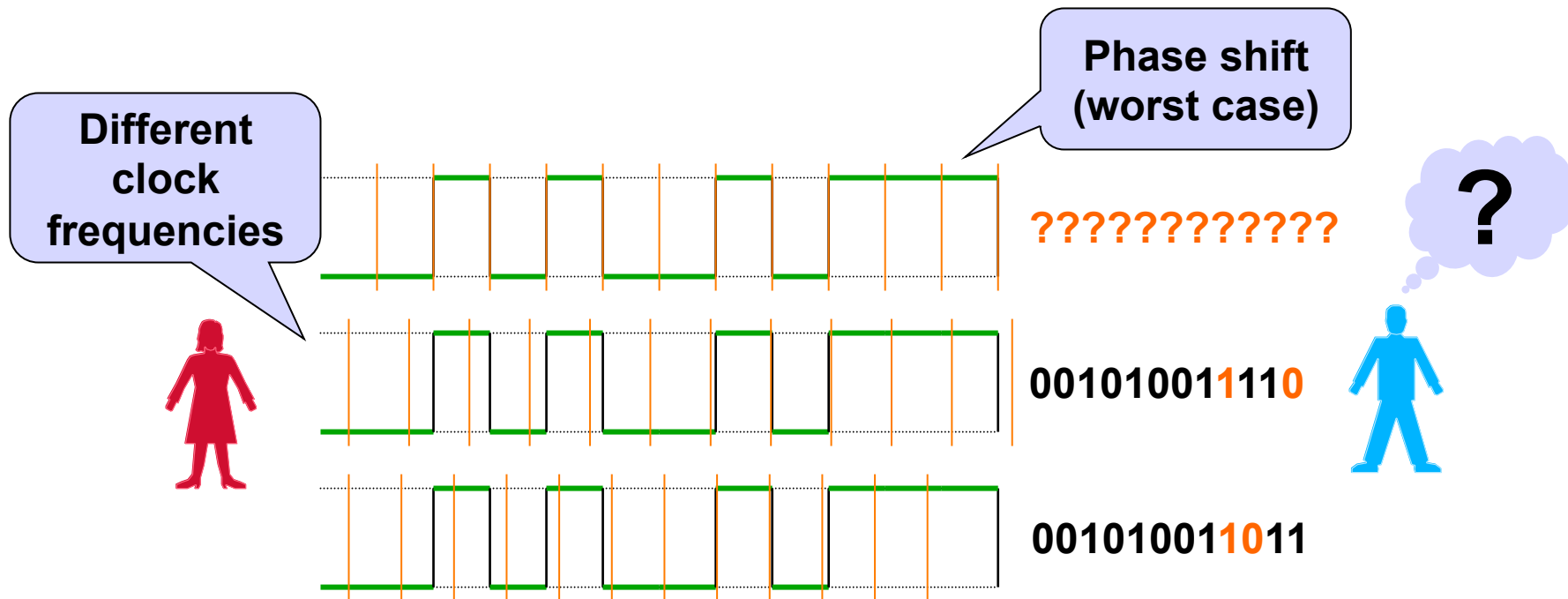
Synchronization

- Sender sends symbol after symbol...
- **When** should receiver pick the signal samples?
 - => Receiver must **sync** with sender's clock !

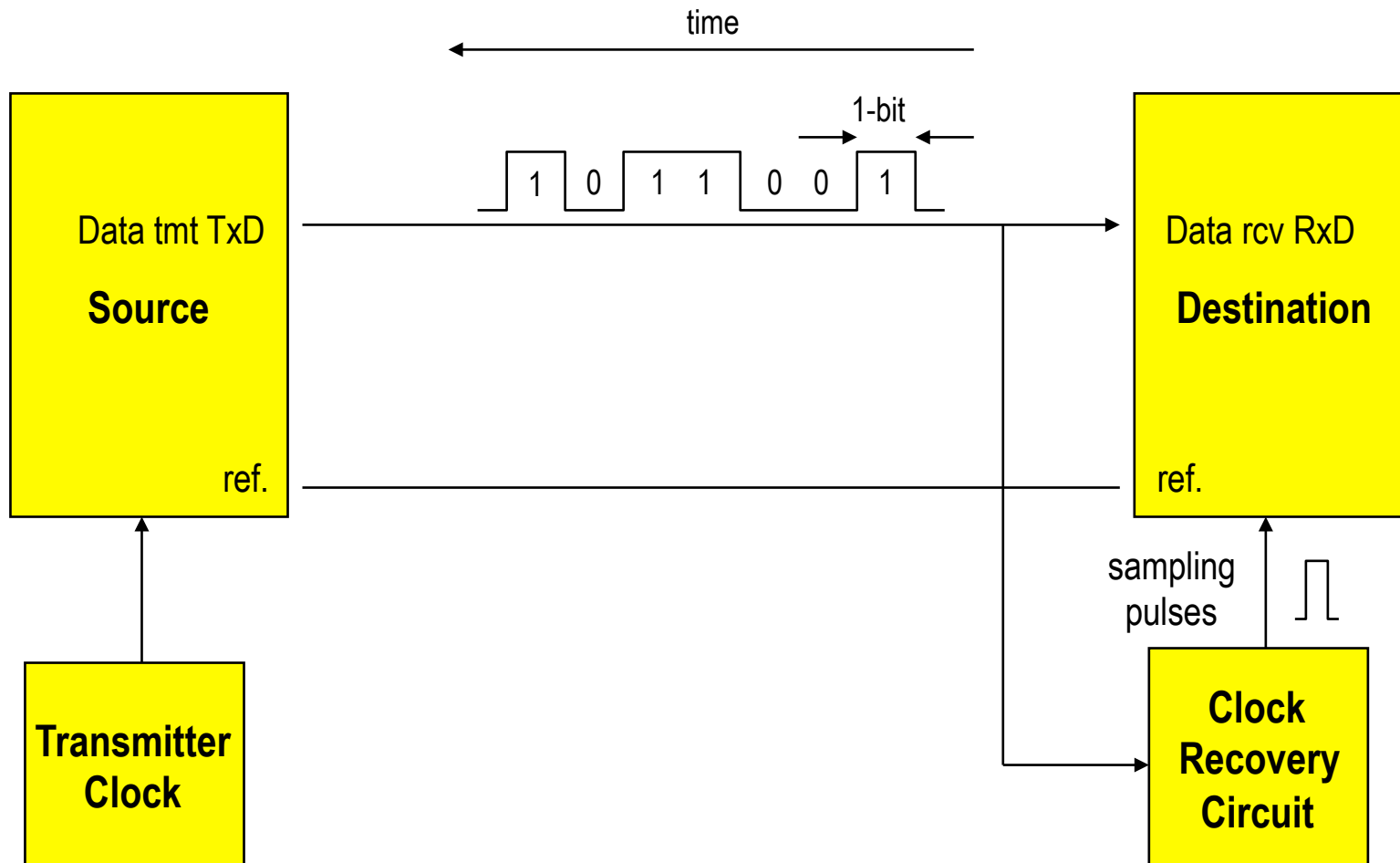


Synchronization

- In reality, two independent clocks are **NEVER** precisely synchronous
 - We always have a frequency shift
 - But we must also care for phase shifts



Bit (Clock) Synchronization Receiver Side

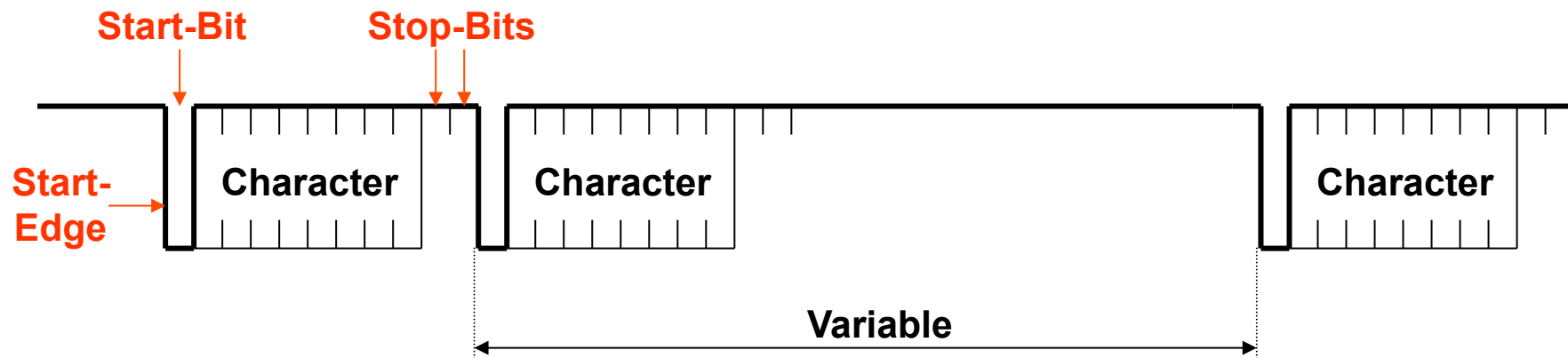


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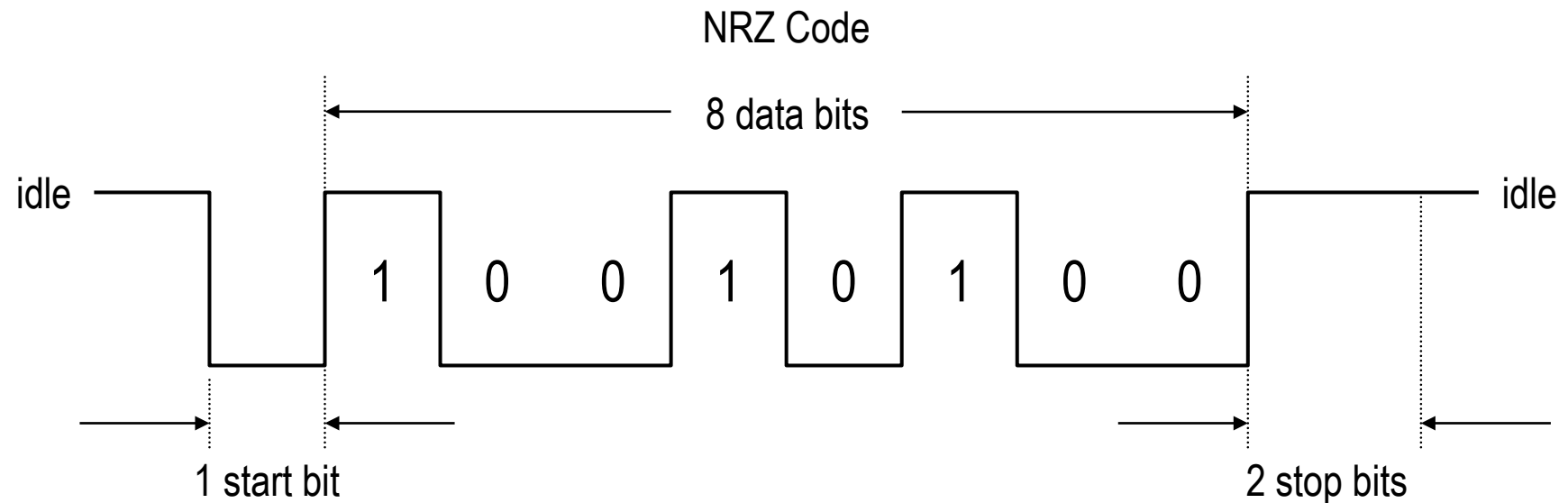
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Asynchronous Transmission

- **Independent clocks at transmitter and receiver**
 - Oversampling at the receiver: Much faster than bit rate
- **Only phase is synchronized**
 - Using Start-bits and Stop-bits
 - Variable intervals between characters
 - Synchronicity only during transmission of a data word
- **Inefficient**
 - 8 bits data need additional 3 bits for bit synchronization

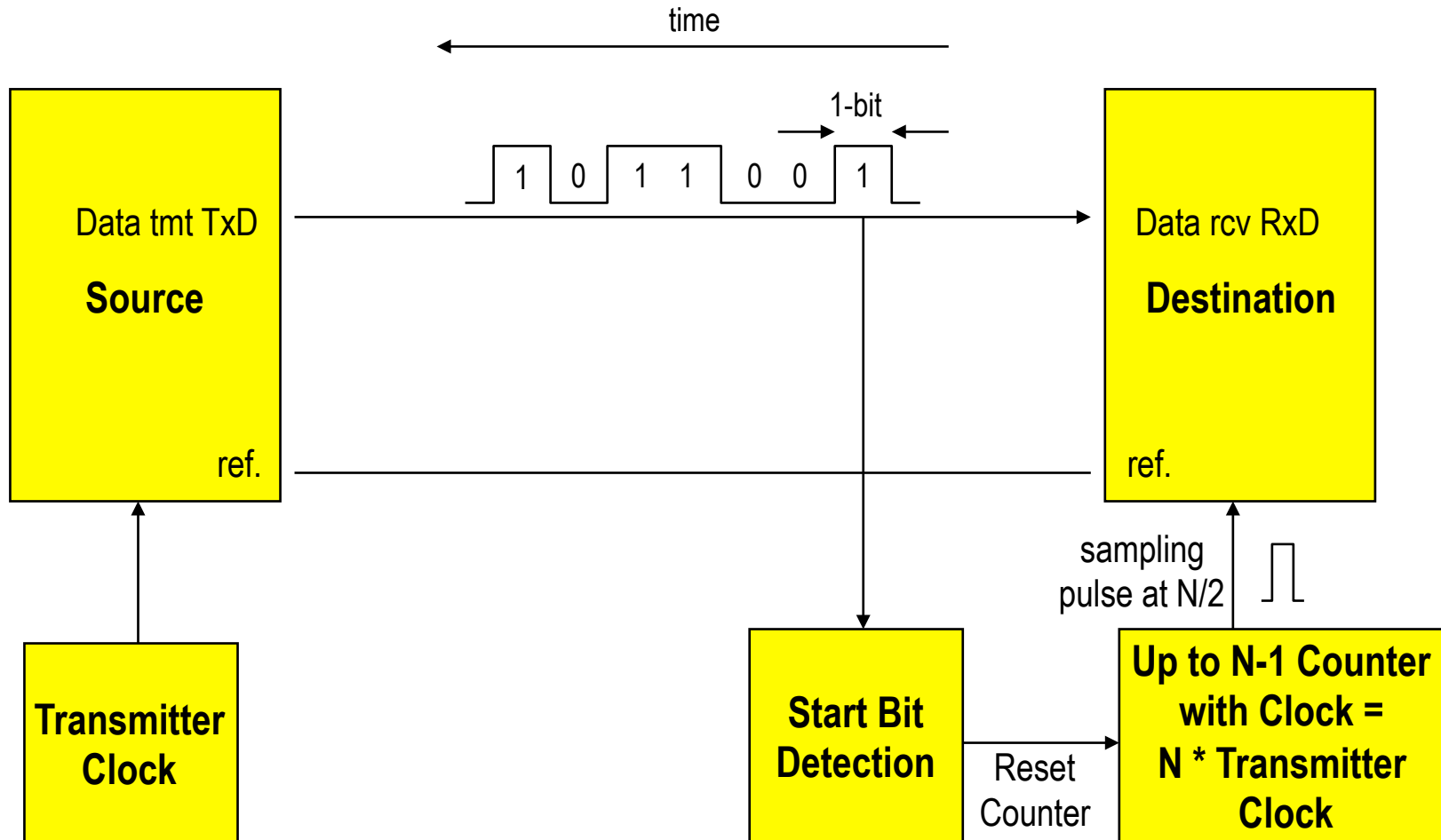


Data Word Framing by Start / Stop Bits



- NRZ (non return to zero) describes the encoding of bits where level 1 refers to logical 1 and level 0 refers to logical 0
- Idle no data is transmitted, no change of signal level

Bit Synchronization Circuit Asynchronous



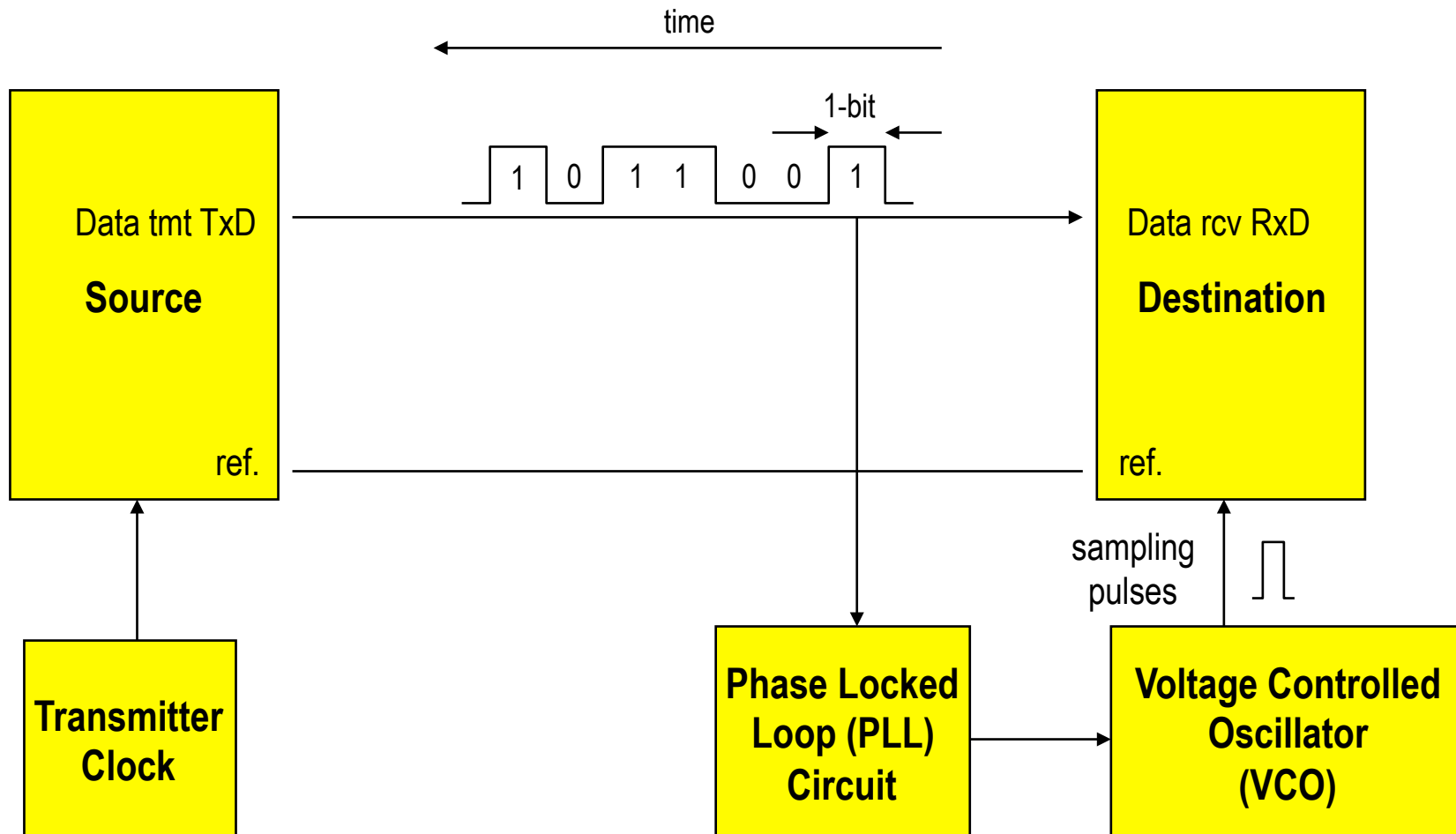
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Synchronous Transmission

- **Synchronized clocks**
 - Most important today!
 - Phase and Frequency synchronized
- **Receiver uses a **Phased Locked Loop (PLL)** control circuit**
 - Requires frequent signal changes
 - => *Coding* or *Scrambling* of data necessary to avoid long sequences without signal changes
 - Encoding / Scrambling at the sender side
 - Decoding / Descrambling at the receiver side
- **Continuous data stream possible**
 - Large frames possible (theoretically endless)
 - Receiver remains synchronized
 - Typically each frame starts with a short "**training sequence**" aka "**preamble**" for the PLL to lock in (e. g. 64 bits)

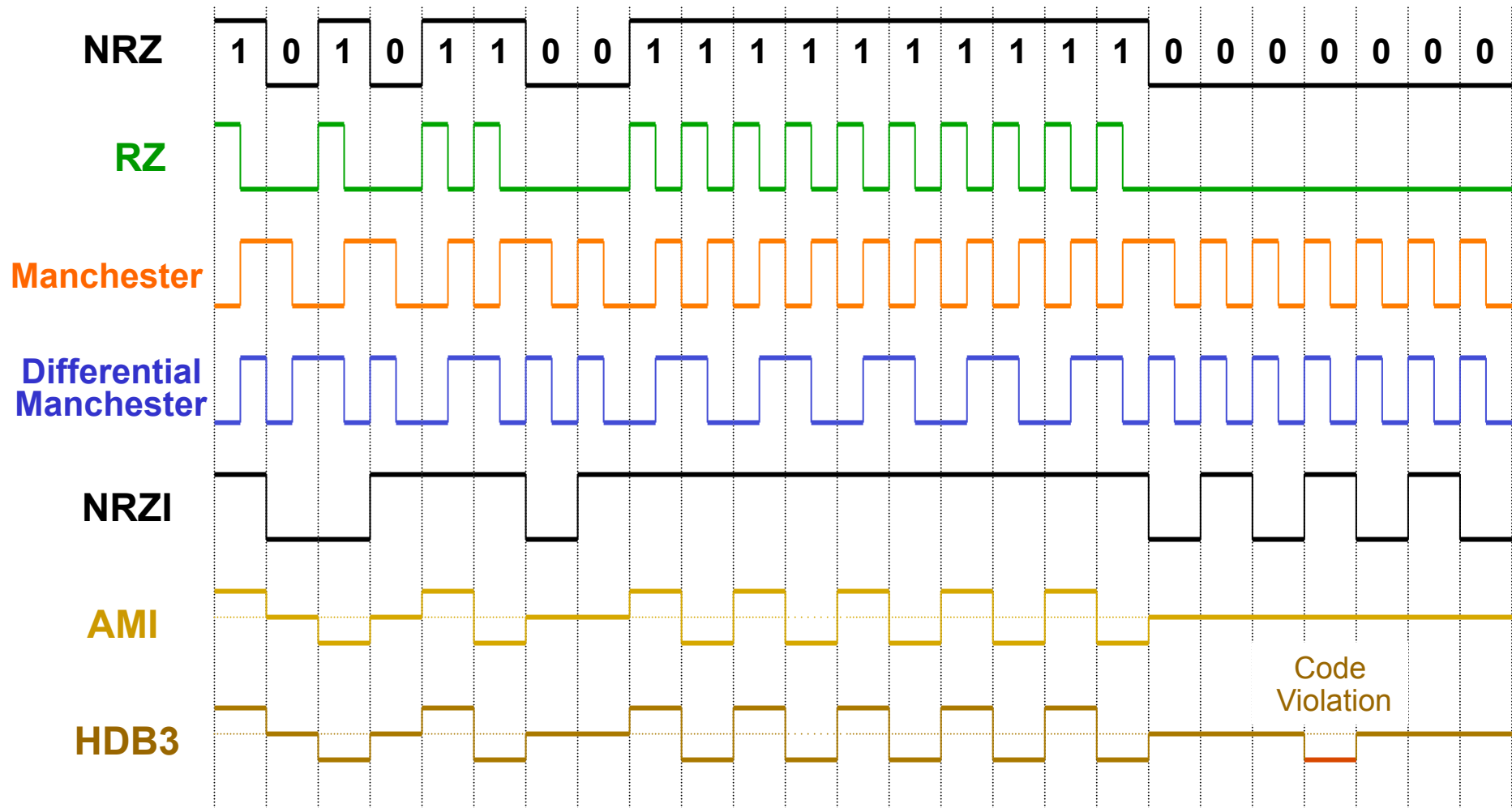
Bit Synchronization Circuit Synchronous



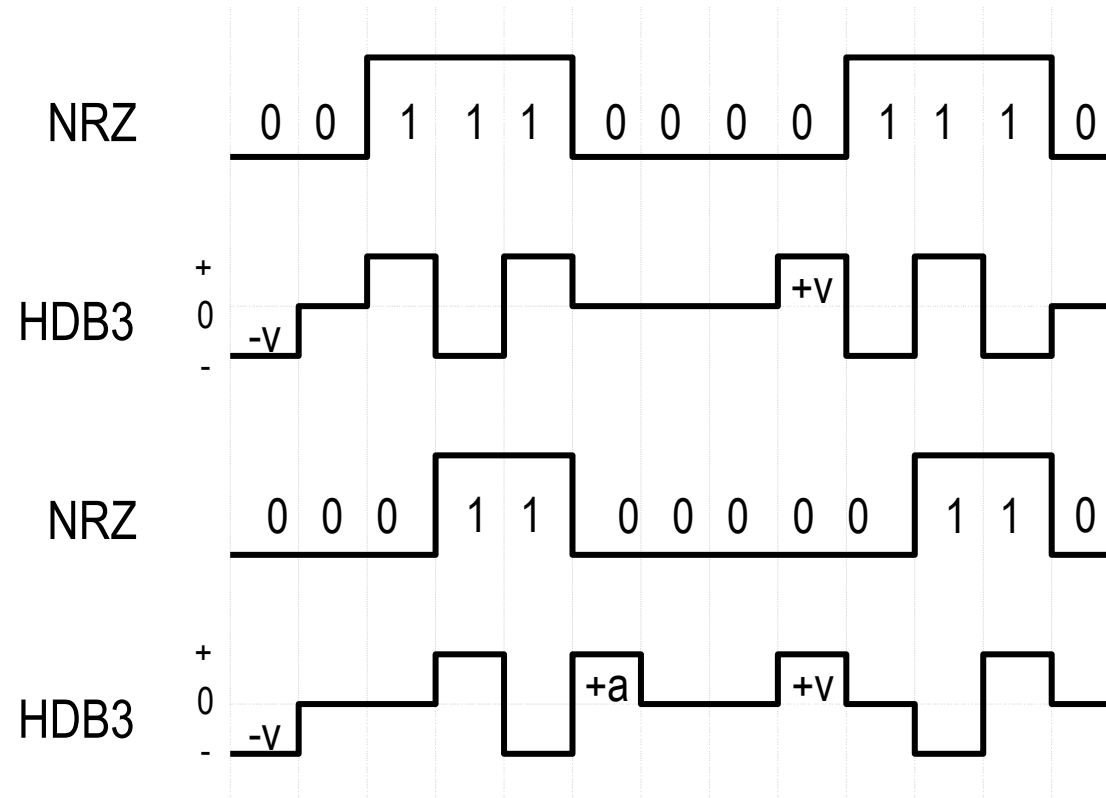
Synchronous Transmission

- **Bit synchronization depends on sufficient signal changes within the bit stream**
 - For long series of 0s or 1s simple NRZ encoding is not able to provide this changes
- **Two basic methods are used to guarantee signal changes**
 - Encoding of bits that every bit contains a signal change
 - Manchester-code (Biphase code), Differential-Manchester-code, commonly used in a LANs
 - Encoding of bits in such a way that there are enough signal changes in the bit stream
 - NRZI (with bitstuffing), RZ and AMI (with scrambler)
 - HDB3 (with code violations), commonly used in a WANs

Line Coding Examples

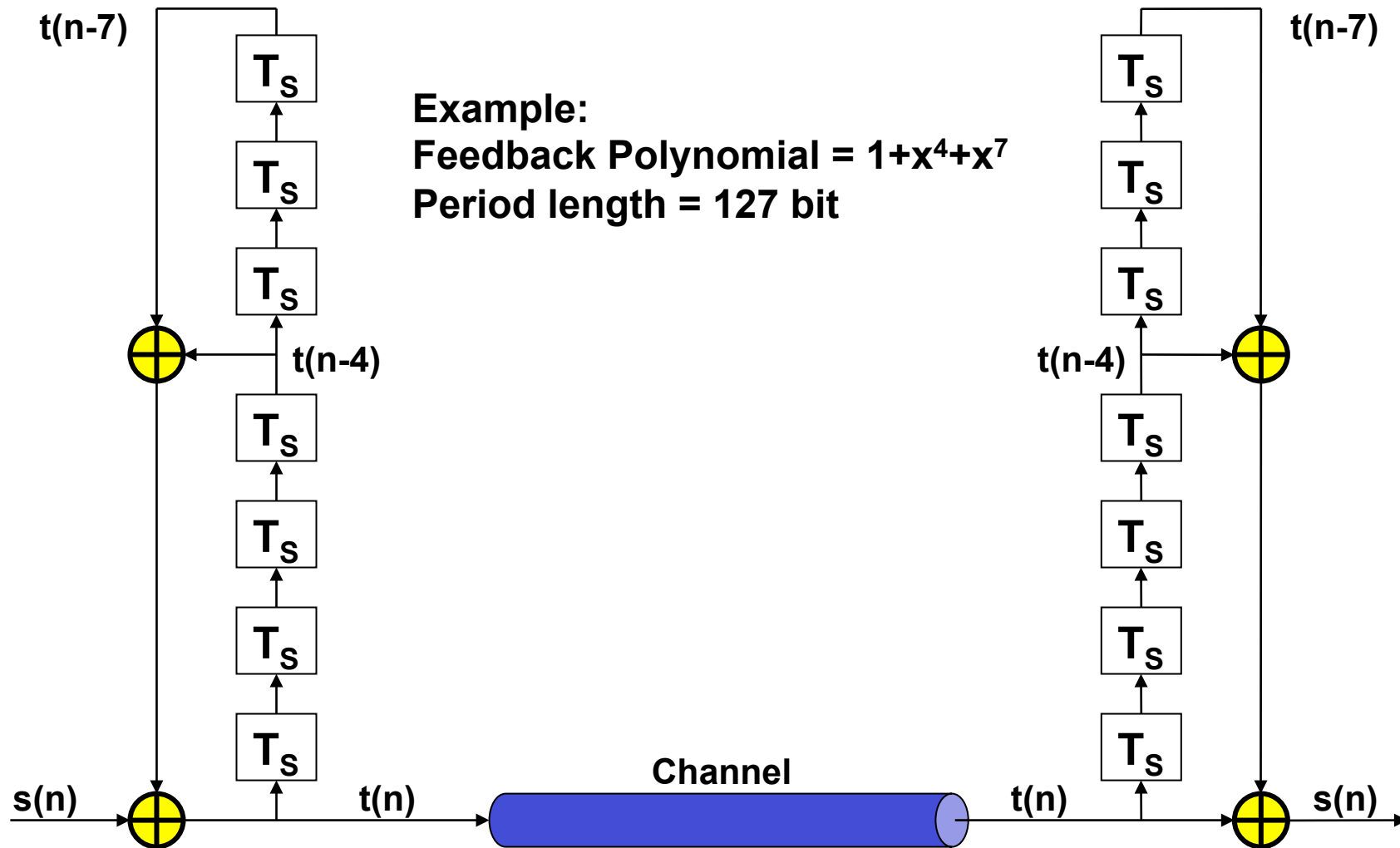


HDB3 (High Density Bipolar 3) Code



bit pattern	polarity of last pulse	amount of pulses since last violation	
	plus minus	odd	even
	plus	0 0 0 +v	-A 0 0 -v
	minus	0 0 0 -v	+A 0 0 +v

How Does a Scrambler Circuit Look Like?



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Theoretical Basis for Data Transmission

- **How can a digital signal be represented?**
 - Fourier analysis proves that any periodic function $g(t)$ with period T can be constructed by summing a (infinite in case of rectangle pulses) number of sinus and cosines functions

$$g(t) = (1/2)c + \sum_{n=1}^{\infty} a_n \sin(2\pi nft) + \sum_{n=1}^{\infty} b_n \cos(2\pi nft)$$

- With $f = 1/T$ and a_n and b_n as amplitudes of the n^{th} harmonics and c as the dc component
- Such a decomposition is called Fourier series

Fourier Coefficients

- How can the values of c , a_n and b_n be computed?

$$c = (2/T) \int_0^T g(t) dt$$

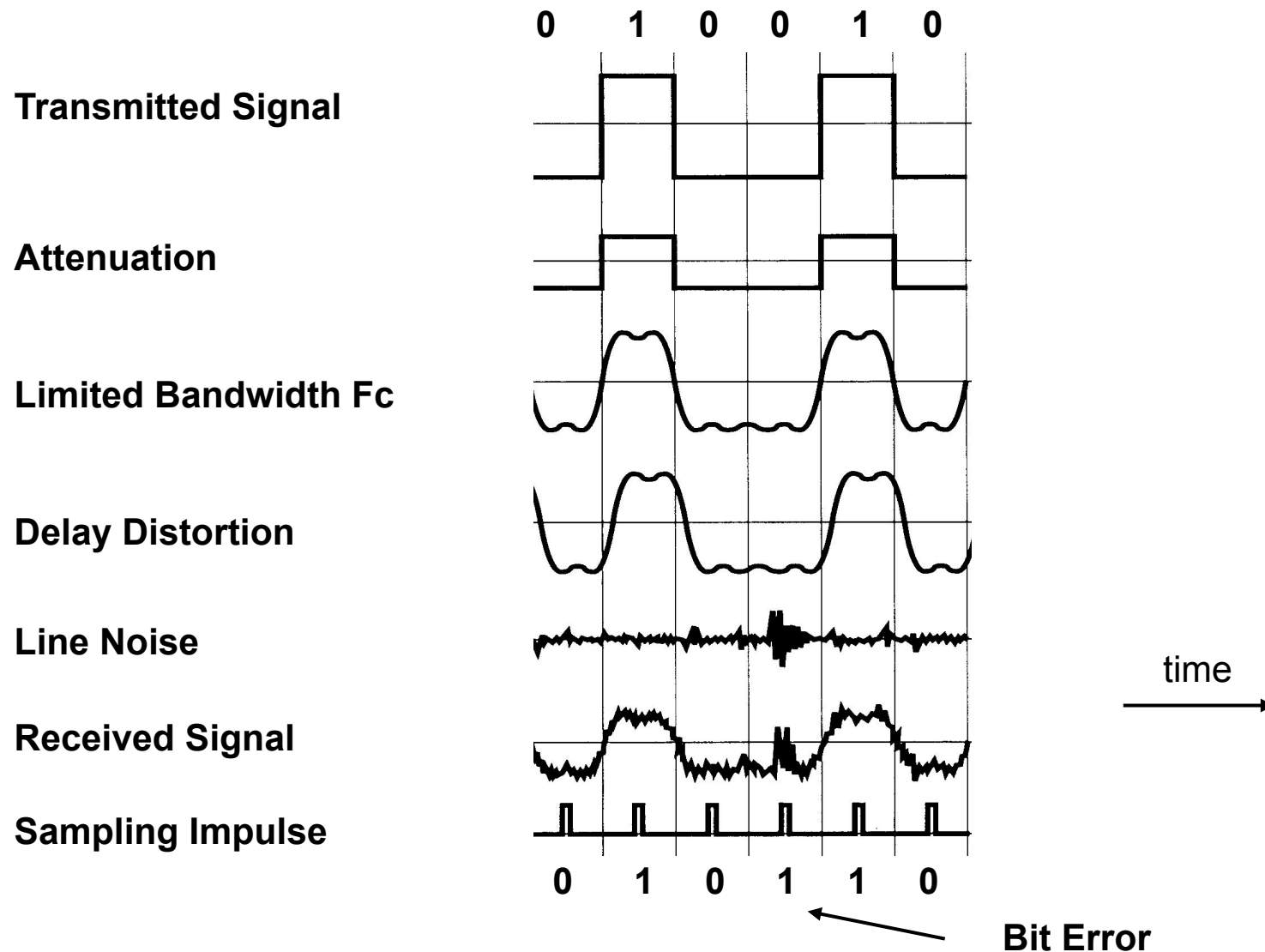
$$a_n = (2/T) \int_0^T g(t) \sin(2\pi nft) dt$$

$$b_n = (2/T) \int_0^T g(t) \cos(2\pi nft) dt$$

Imperfect Real Data Transmission

- 1. No transmission systems can transmit signals without losing some power (attenuation)**
- 2. No transmission systems can transmit different Fourier components with the same speed (delay distortion)**
- 3. No transmission systems is free from noise**

That Happens To A Signal !!!



Real Data Transmission

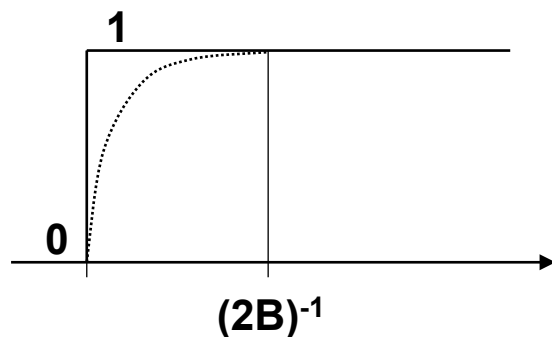
- **In real transmission systems**
 - The original signal will be attenuated, distorted and influenced by noise when traversing the transmission line
- **By increasing the bit rate**
 - Bit synchronization even in middle of a bit becomes more and more difficult because of these impairments
 - Above a certain rate bit synchronization will be impossible
- **Relationship**
 - Between bandwidth F_c , line length and maximum achievable bit rate on a certain transmission line (system)

Maximal Information Rate (Theoretical)

- **What is the maximal information rate of an ideal (noiseless) but bandwidth limited transmission channel ?**
 - Nyquist law: $R = 2 * B * \log_2 V$
 - valid for a noiseless channel
 - R ... maximum bit rate (bits/sec)
 - B ... bandwidth range of a bandwidth limited transmission
 - V ... number of signal levels (e.g. 2 for binary transmission)
 - example analogue telephone line
 - B = 3000 Hz (range 400 – 3400 Hz)
 - R = 6000 bits/sec for V = 2
 - R = 18000 bits/sec for V = 8

Nyquist Law Rationale

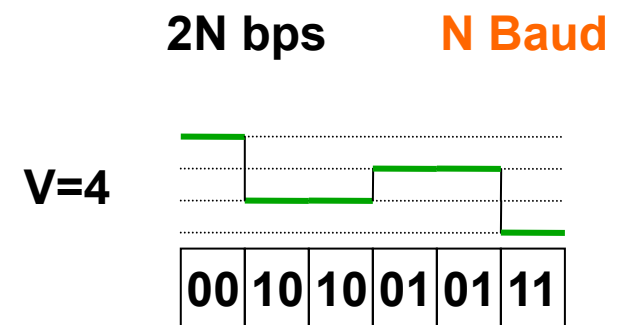
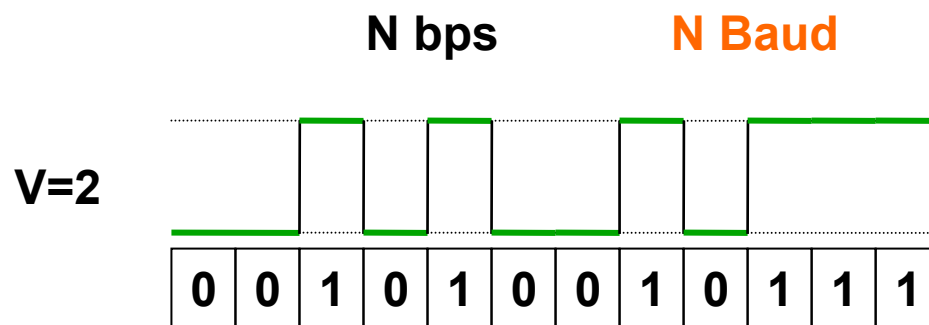
- **Maximal data rate proportional to channel-bandwidth B**
 - Raise time of Heavyside $T=1/(2B)$
 - **So the maximum rate is $R=2B$** , also called the Nyquist Rate
 - Note: We assume an ideal channel here – without noise!
- **Bandwidth decreases with cable length**
 - As a dirty rule of thumb: $BW \times \text{Length} \cong \text{const}$
 - But note that the reality is much more complex
 - Solitons are remarkable exceptions...



Maximum signal rate: At least the amplitude must be reached

Bitrate versus Baud

- **The rate of changes of a symbol**
 - is called signaling rate R_s or **Symbol Rate**
 - is measured in Baud
- **The rate of bits transported**
 - is called bit rate R_i or **Information Rate**
 - and is measured in bit/sec (bps)
- $R_i = R_s * \log_2 V$
 - V ... number of signal levels
- $R_i = R_s$
 - for binary transmission where $V = 2$
- **The goal is to send many (=as much as possible) bits per symbol**
 - => QAM (see next slides)



Maximal Information Rate (Reality)

- **What about a real channel? What is the maximum achievable information rate in presence of noise?**
 - Disturbance caused by crosstalk, impulse noise, thermal or white noise
- **Answer by C. E. Shannon in 1948**
 - Even when noise is present, information can be transmitted *without errors* when the information rate is below the *channel capacity C*
 - Channel capacity depends only on channel bandwidth and SNR (signal to noise ratio)
 - $\max R = C = B * \log_2 (1+S/N)$
 - S ... signal power, N ... noise power
 - SNR ... measured in decibel (db)
 - $SNR = 10 * \log_{10} S/N$
 - example analogue telephone line
 - B = 3000 Hz
 - SNR = 30 db means $30 = 10 * \log_{10} (S/N) \rightarrow S/N = 1000$
 - $\max R = 3000 * \log_2 (1+1000) = 3000 * (9,967226259)$
 - $\max R =$ approximately 29902 bits/sec

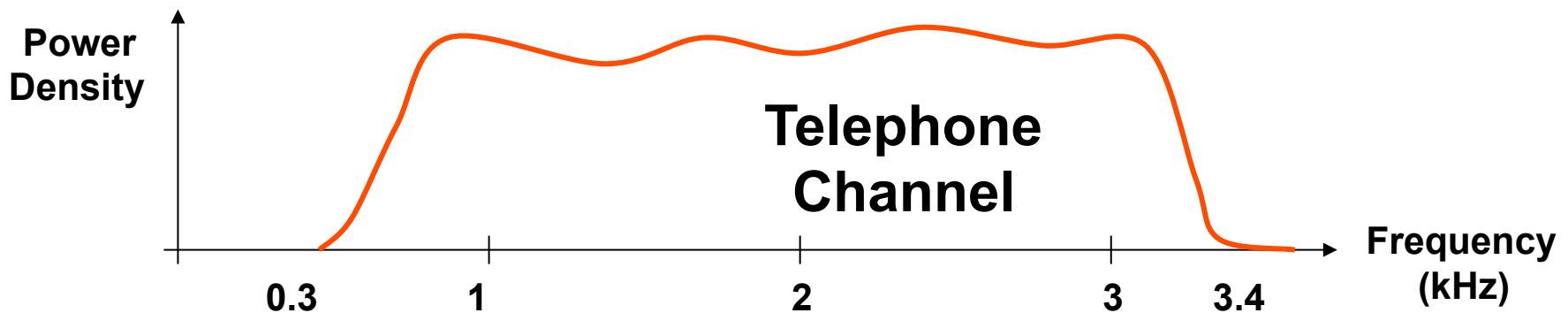
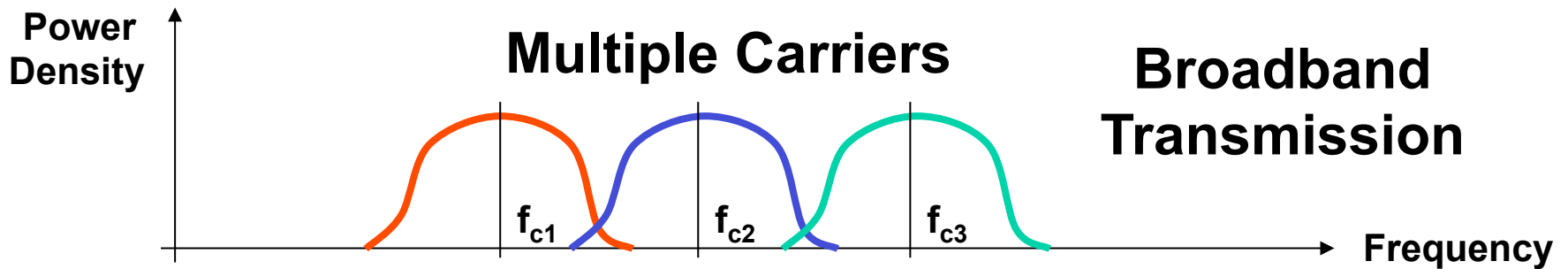
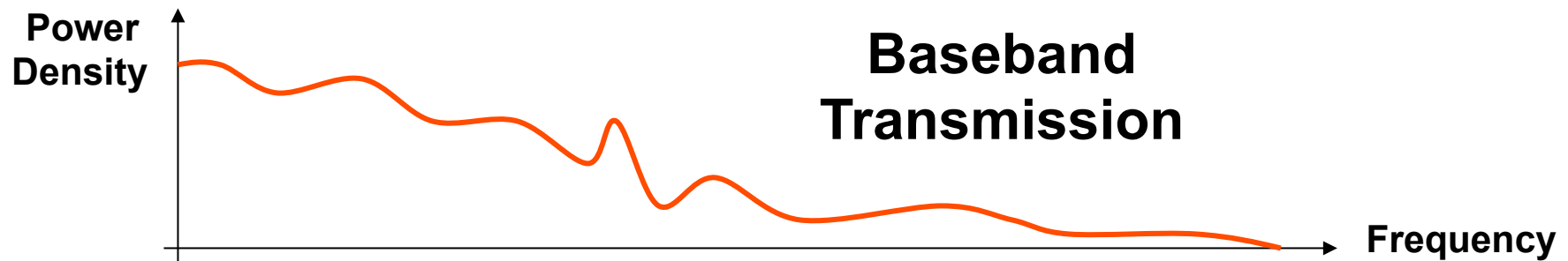
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Communication Channels

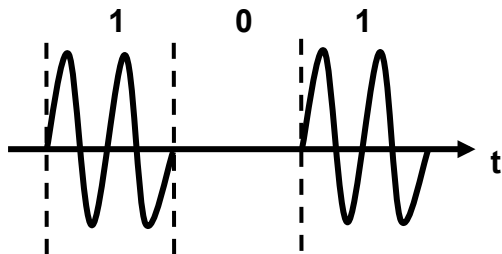
- Usually **Low-Pass** behavior
 - Higher frequencies are more attenuated than lower
- **Baseband transmission**
 - Signal without a dedicated carrier
 - Example: LAN technologies (Ethernet etc)
- **Carrierband / Narrowband transmission**
 - The baseband signal modulates a carrier to match special channel properties
- **Broadband transmission**
 - Different baseband signals modulate different carriers
 - Medium can be shared for many users / channels e. g. WLAN and cable networks

Channel Utilization Examples

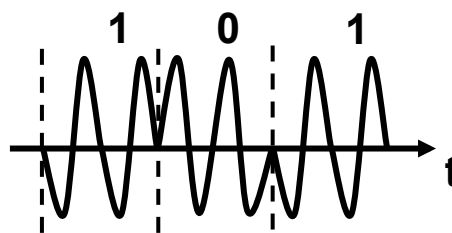


Analogue Modulation Overview

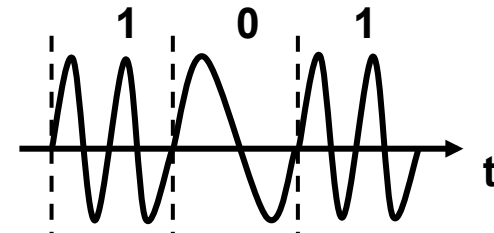
- **EVERY transmission is analogue – but there are different methods to put a base-band signal onto a high-frequency carrier**
- **The most simple (and oldest) is ASK**
 - The illustrated ASK method is simple "On-Off-Keying" (OOK)
- **FSK and PSK are called "angle-modulation" methods (nonlinear => spectrum shape is changed!)**
- **For digital transmission, almost always QAM is used**
 - The BER of BPSK is 3 dB better than for simple OOK



Amplitude Shift Keying (ASK)



Phase Shift Keying (PSK)



Frequency Shift Keying (FSK)

$$g(t) = A_t \cdot \cos(2\pi f_t t + \varphi_t)$$

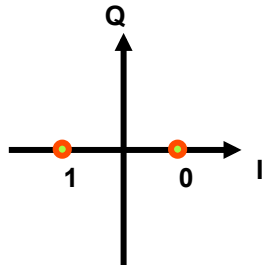
These three parameters can be modulated

QAM: Idea

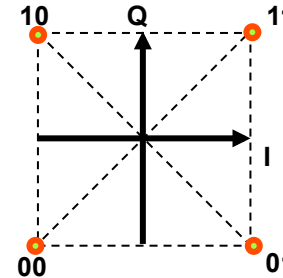
- **"Quadrature Amplitude Modulation"**
- **Idea:**
 1. Separate bits in groups of words (e. g. of 6 bits in case of QAM-64)
 2. Assign a dedicated pair of Amplitude and phase to each word (A, φ)
 3. Create the complex amplitude $Ae^{j\varphi}$
 4. Create the signal $\text{Re}\{Ae^{j\varphi} e^{j\omega t}\}$
 $= A (\cos \varphi \cos \omega t - \sin \varphi \sin \omega t)$ which represents one (of the 64) QAM symbols
 5. Receiver can reconstruct (A, φ)

QAM: Symbol Diagrams

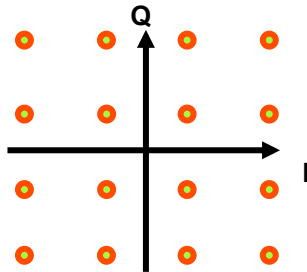
Standard PSK



Quadrature PSK (QPSK)

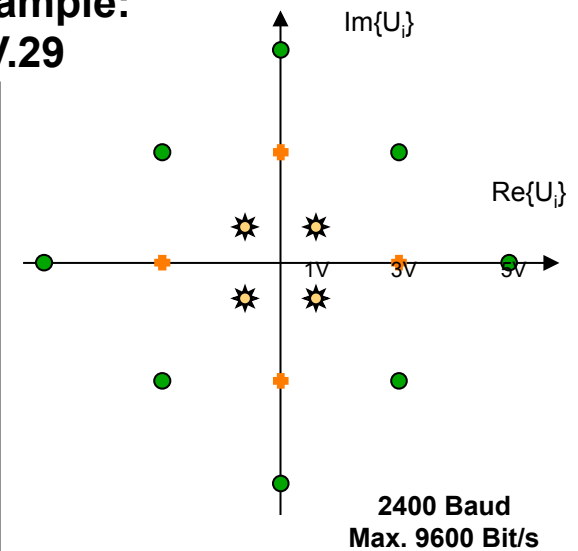


16-QAM

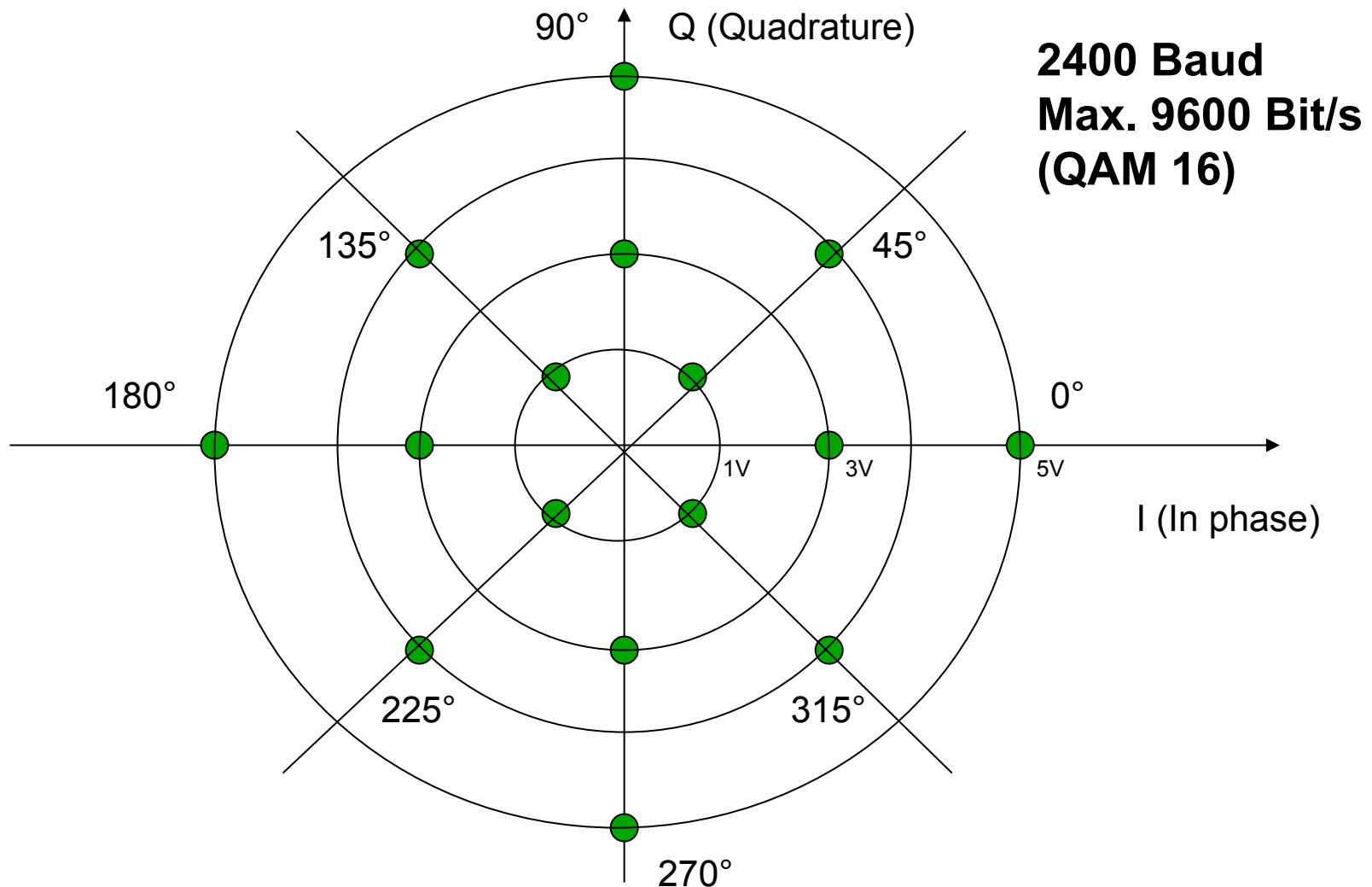


Other example:
Modem V.29

+ For noisy and distorted channels
4800 bit/s
* For better channels
7200 bit/s
● For even better channels
9600 bit/s



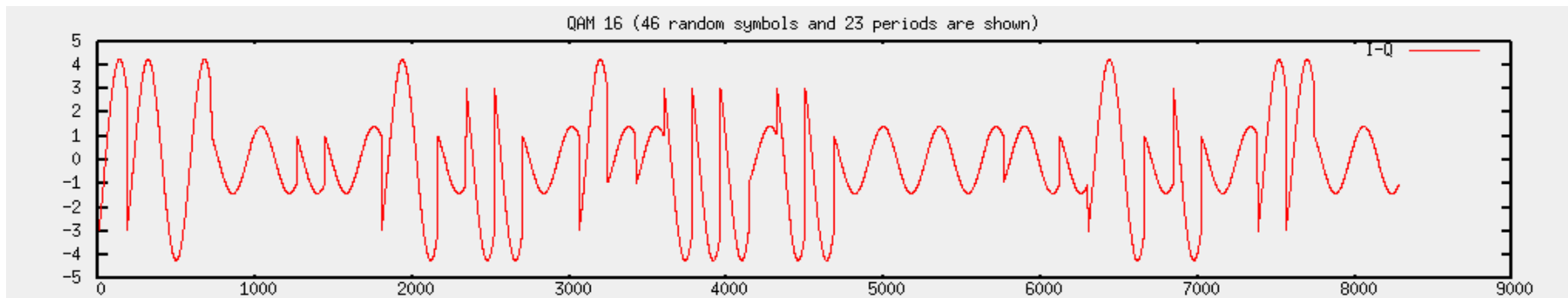
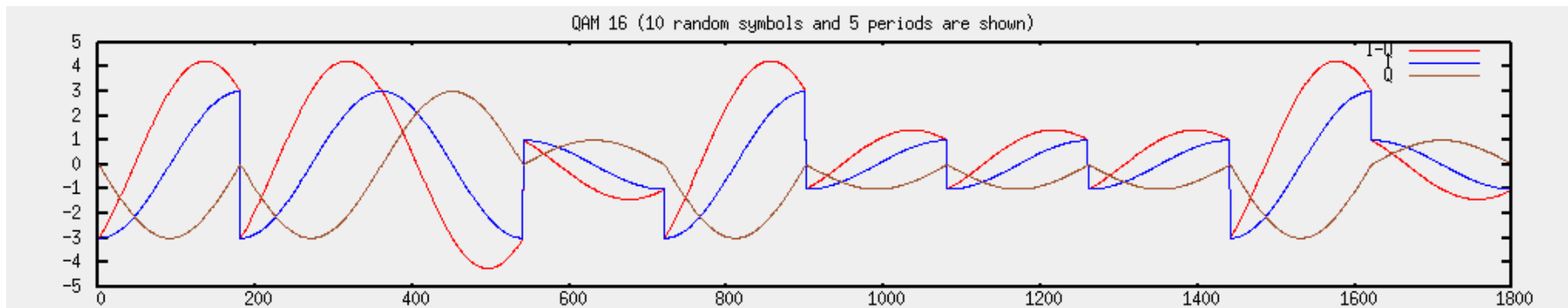
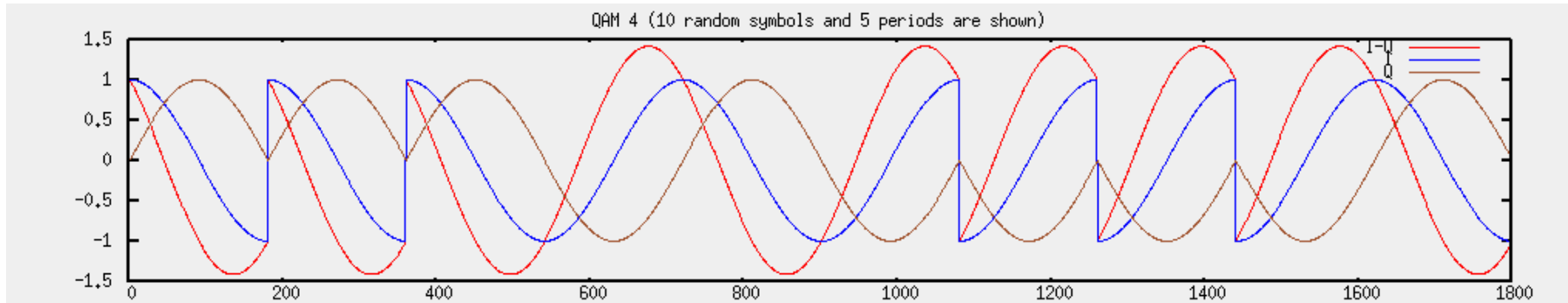
Modem: V.29 (QAM) for TELCO Lines



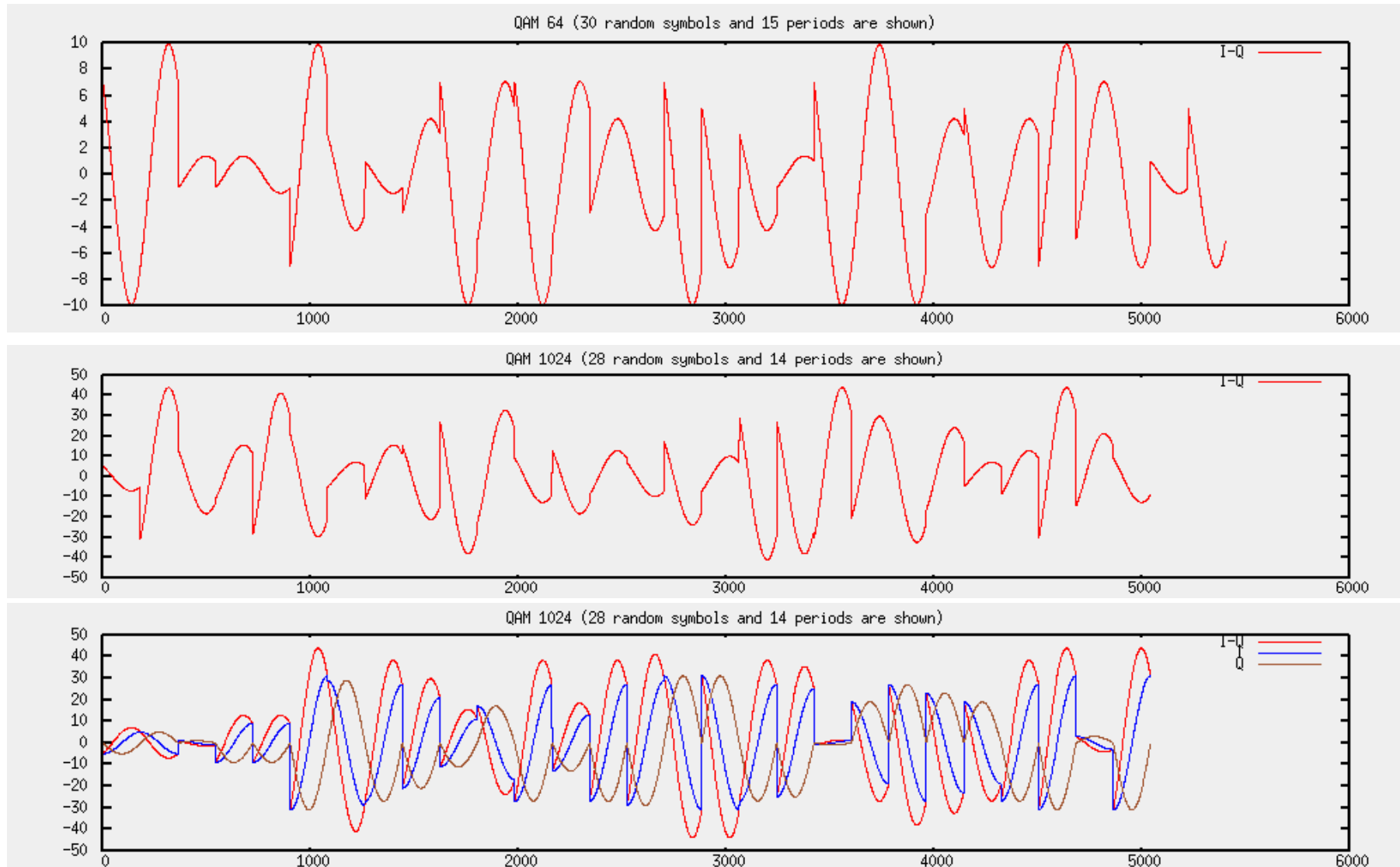
Example QAM Applications

- **One symbol represents a bit pattern**
 - Given N symbols, each represent $\log_2(N)$ bits
- **Modems (Telco – 200-3500Hz limited),**
- **1000BaseT (Gigabit Ethernet)**
- **WiMAX, GSM, ...**
- **WLAN 802.11a and 802.11g:**
 - BPSK @ 6 and 9 Mbps
 - QPSK @ 12 and 18 Mbps
 - 16-QAM @ 24 and 36 Mbps
 - 64-QAM @ 48 and 54 Mbps

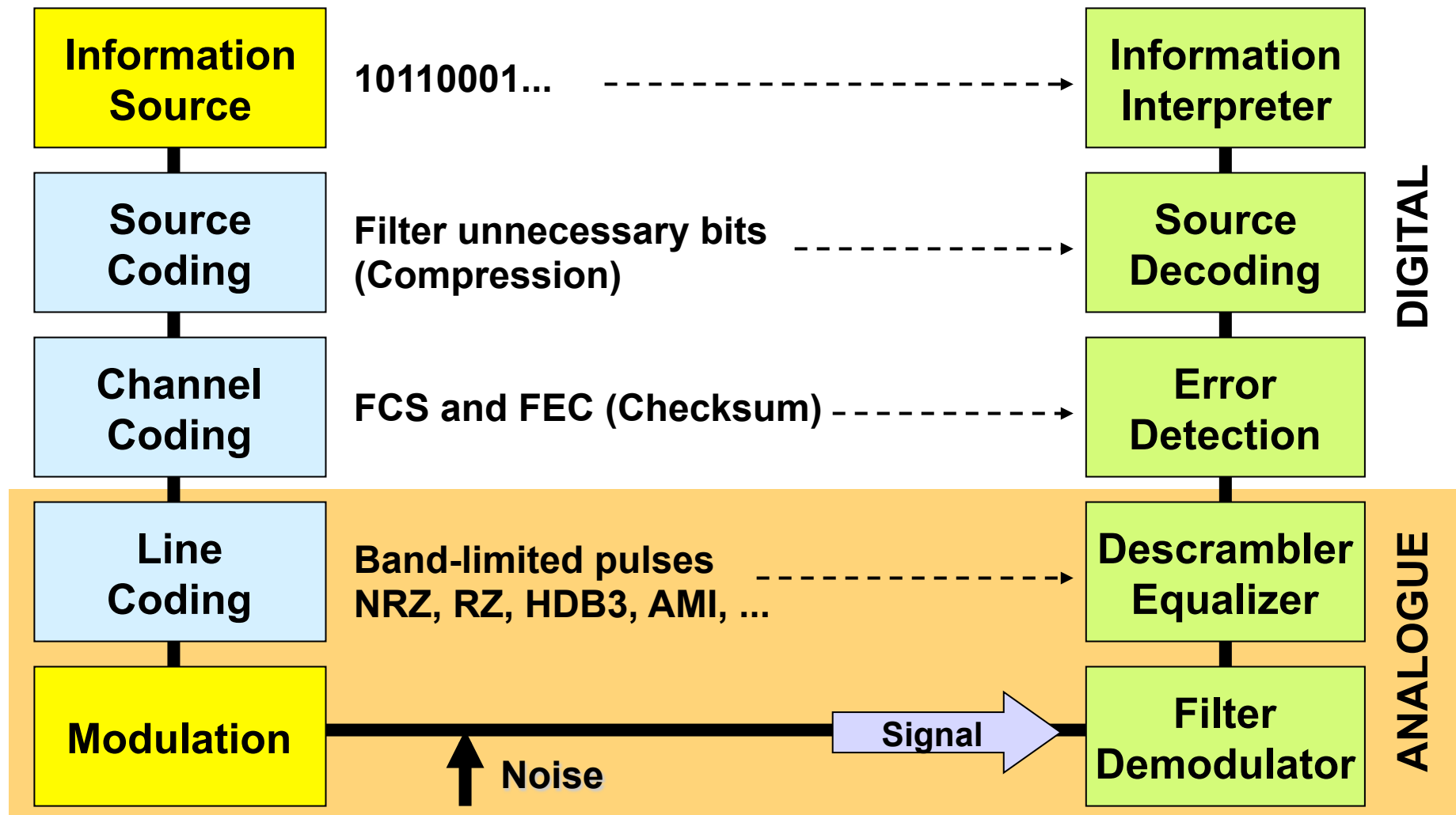
QAM Example Symbols (1)



QAM Example Symbols (2)



Transmission System Summary



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Time to Transmit A Given Number Of Bytes

$$\text{Serialization Delay (in ms)} = [(\text{Number of Bytes} * 8) / (\text{Bitrate in sec})] * 1000$$

	Bitrate	9,6 kbit/s	48 kbit/s	128 kbit/s	2,048 Mbit/s	10 Mbit/s	100 Mbit/s	155 Mbit/s	622 Mbit/s	1 Gigabit/s
	Number of Byte	Delay in msec (10 ⁻³)	Delay in msec (10 ⁻³)	Delay in msec (10 ⁻³)	Delay in msec (10 ⁻³)	Delay in msec (10 ⁻³)	Delay in msec (10 ⁻³)	Delay in msec (10 ⁻³)	Delay in msec (10 ⁻³)	Delay in msec (10 ⁻³)
Bit	0,125	0,104167	0,020833	0,007813	0,000488	0,000100	0,000010	0,000006	0,000002	0,000001
Byte	1	0,833333	0,166667	0,062500	0,003906	0,000800	0,000080	0,000052	0,000013	0,000008
PCM-30	32	26,666667	5,333333	2,000000	0,125000	0,025600	0,002560	0,001652	0,000412	0,000256
ATM cell	53	44,166667	8,833333	3,312500	0,207031	0,042400	0,004240	0,002735	0,000682	0,000424
Ethernet	64	53,333333	10,666667	4,000000	0,250000	0,051200	0,005120	0,003303	0,000823	0,000512
X.25	256	213,333333	42,666667	16,000000	1,000000	0,204800	0,020480	0,013213	0,003293	0,002048
IP	576	480,000000	96,000000	36,000000	2,250000	0,460800	0,046080	0,029729	0,007408	0,004608
Ethernet	1.518	1.265,000000	253,000000	94,875000	5,929688	1,214400	0,121440	0,078348	0,019524	0,012144
FR	8.192	6.826,666667	1.365,333333	512,000000	32,000000	6,553600	0,655360	0,422813	0,105363	0,065536
TCP	65.534	54.611,666667	10.922,333333	4.095,875000	255,992188	52,427200	5,242720	3,382400	0,842881	0,524272

1kbit/s = 1000 bit/s !!!
 1KByte = 1024 Byte !!!

Propagation (Signal) Delay

$$T_p = \text{Propagation Delay (in ms)} = [(\text{Distance in m}) / (\text{velocity in m/sec})] * 1000$$

	Distance	v=200.000km/s Delay in msec (10 ⁻³)	v=300.000km/s Delay in msec (10 ⁻³)
CPU Bus	10 cm	0,0000005	0,0000003
	1 m	0,0000050	0,0000033
RS232, V24/V.28	15 m	0,0000750	0,0000500
LAN, Copper, RJ45	100 m	0,0005000	0,0003333
LAN, FO, X.21/V.11-V.10	1 km	0,0050000	0,0033333
Local Subscriber Line	2,5 km	0,0125000	0,0083333
WAN Link Repeater	10 km	0,0500000	0,0333333
WAN Link Repeater	100 km	0,5000000	0,3333333
WAN FO Link Repeater	1.000 km	5,0000000	3,3333333
WAN FO Link Repeater	10.000 km	50,0000000	33,3333333
Satellite Link	40.000 km	200,0000000	133,3333333
Satellite Link	50.000 km	250,0000000	166,6666667
	100.000 km	500,0000000	333,3333333
	300.000 km	1500,0000000	1000,0000000

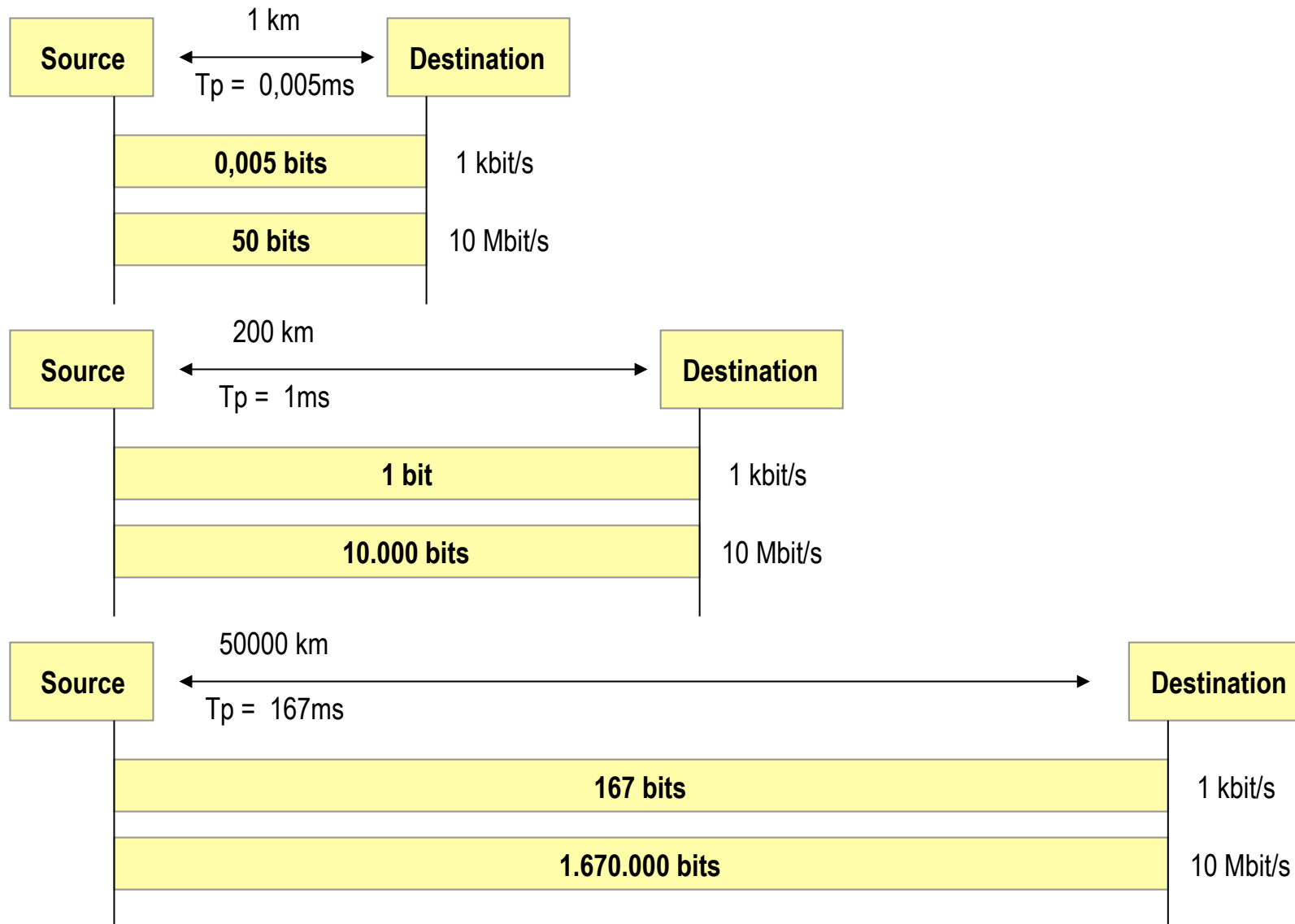
Total Delay (for a block of bits)
= Serialization Delay + Propagation Delay + (Switching Delay)

How Long Is A Bit?

$$\text{Length (in m)} = [(1 / (\text{bitrate per sec})] * [(\text{velocity in m/sec})]$$

	Bitrate	Bit Length in meter	Bit Length in meter
Analogue Modem	9,6 kbit/s	20833,33	31250,00
Analogue Modem	48 kbit/s	4166,67	6250,00
DS0	64 kbit/s	3125,00	4687,50
ISDN (2B)	128 kbit/s	1562,50	2343,75
PCM-30, E1	2,048 Mbit/s	97,66	146,48
Token Ring 4	4 Mbit/s	50,00	75,00
Ethernet	10 Mbit/s	20,00	30,00
Token Ring16	16 Mbit/s	12,50	18,75
Fast Ethernet, FDDI	100 Mbit/s	2,00	3,00
ATM STM1, OC-3	155 Mbit/s	1,29	1,94
ATM STM4, OC-12	622 Mbit/s	0,32	0,48
Gigabit Ethernet	1 Gigabit/s	0,20	0,30
OC-48	2,5 Gigabit/s	0,08	0,12
10 Gigabit Ethernet	10 Gigabit/s	0,02	0,03
		Copper	LWL - Free Space
		200.000 km /sec	300.000 km / sec

Propagation Delay And Number Of Bits On A Given Link



Agenda

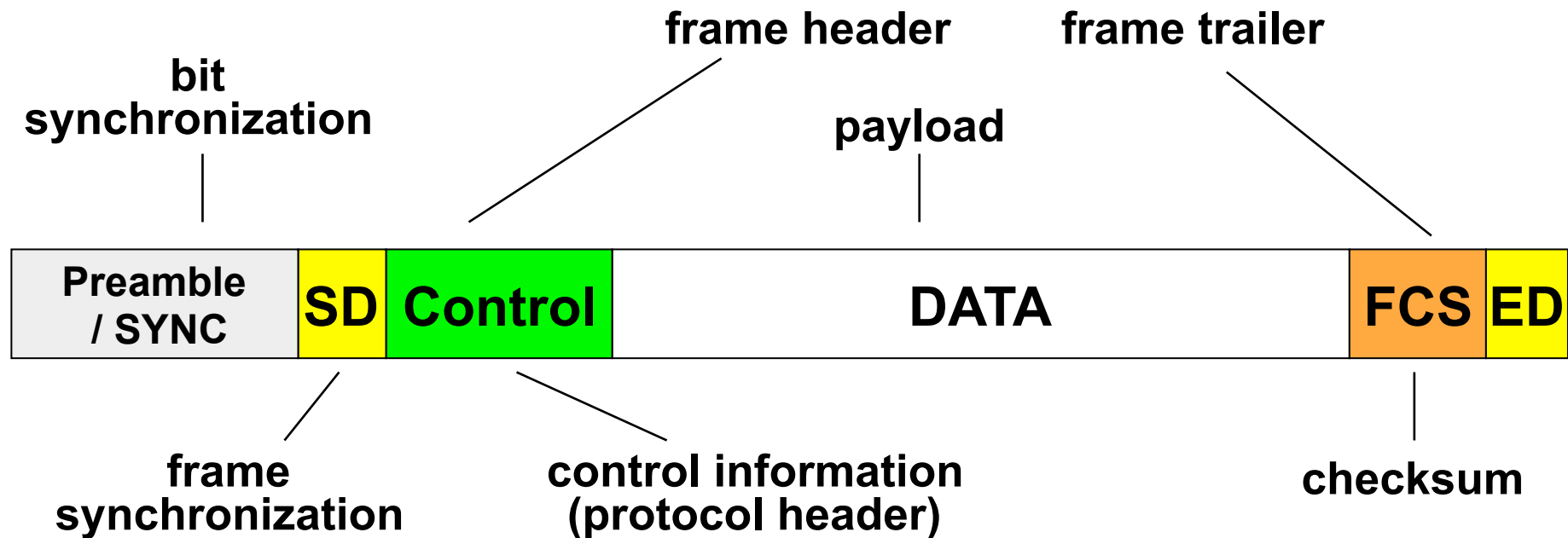
- **Introduction**
- **Bit Synchronization**
 - Asynchronous
 - Synchronous
- **Physical Aspects**
 - Mathematical Background
 - Communication Channel / Modulation
 - Serialization / Propagation Delay
- **Transmission Frame**
 - Generic Format
 - Frame Synchronization
 - Error Control

Requirements & Facts

Serial Transmission System

- **Information between systems is exchanged in blocks of bits**
 - Every block is carried in as so called transmission frames
- **The recognition of the beginning and the end of a block in the received bit stream is necessary**
 - Frame synchronization
- **Errors on physical lines may lead to damage of digital information**
 - 0 becomes 1 and vice versa
 - The longer the block the higher the probability for an error
- **Methods necessary for error checking**
 - Frame protection
 - Error detection and recovery

Generic Frame Format



SYNC- Sync Pattern ED - Ending Delimiter
SD - Starting Delimiter FCS - Frame Check Sequence

Preamble

- **Preamble / SYNC is a special bit pattern**
 - Used for bit synchronization after an idle period (Preamble)
 - Can be used as fill pattern during idle times to keep the receiver clock synchronized (SYNC)
- **Enables PLL synchronization**
 - Typically a 0101010...-pattern
 - Example: 8 Byte preamble in Ethernet frames



Control Field

- **Is used for implementing protocol procedures**
- **Contains information such as**
 - Frame type, protocol type
 - Data, Ack, Nack, Connect, Disconnect, Reset, etc.
 - IP, IPX, AppleTalk, etc.
 - Sequence numbers for identification of frame sequence
 - Necessary for error recovery and flow control with connection oriented services
 - Address information of source and destination in case of a multipoint line
 - Frame length, etc.

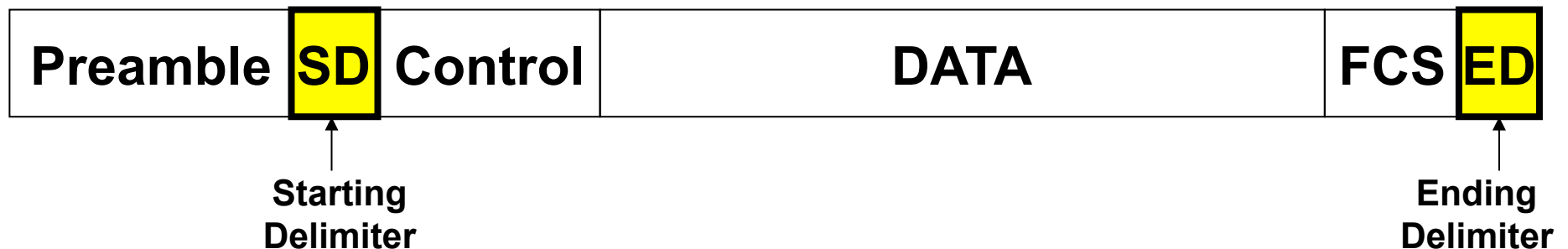


Agenda

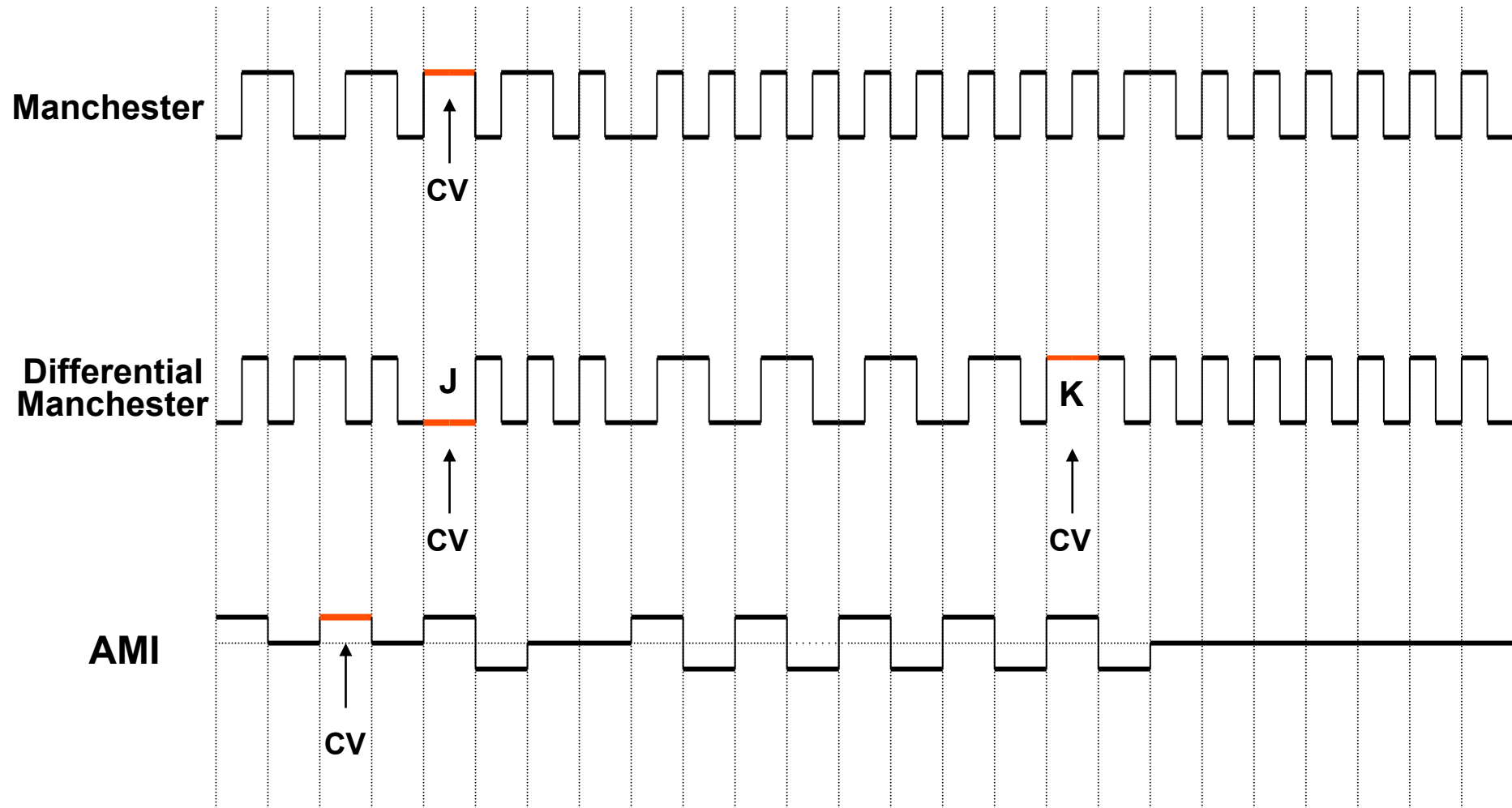
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Frame Synchronization

- **Beginning and ending of a frame is indicated by SD and ED symbols**
 - Bit-patterns or code-violations
 - Length-field can replace ED (802.3)
 - Idle-line can replace ED (Ethernet)
- **Also called "Framing"**

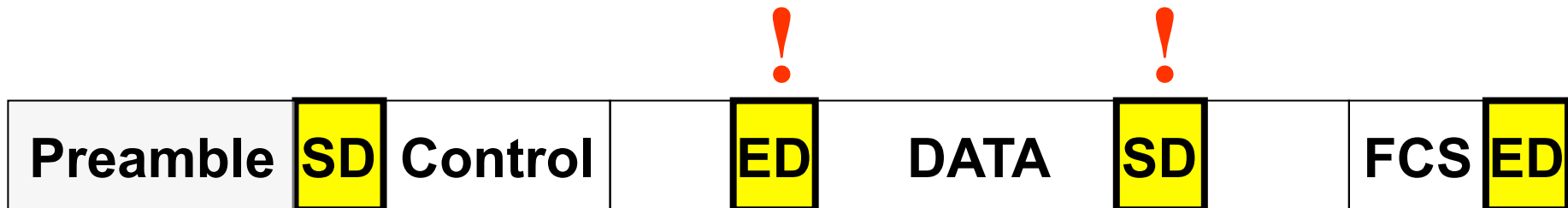


Examples For Code Violations



Protocol Transparency

- What, if delimiter symbols SD, ED occur within frame?
- Solution:
 - Byte-Stuffing
 - Bit-Stuffing



Character-Oriented Transmission ASCII-Code

American Standard Code for Information Interchange

Bit Positions	7	0	0	0	0	1	1	1	1
	6	0	0	1	1	0	0	1	1
	5	0	1	0	1	0	1	0	1
0 0 0 0	Nul	DLE	SP	0	@	P	\	p	
0 0 0 1	SOH	DC1	!	1	A	Q	a	q	
0 0 1 0	STX	DC2	"	2	B	R	b	r	
0 0 1 1	ETX	DC3	#	3	C	S	c	s	
0 1 0 0	EOT	DC4	\$	4	D	T	d	t	
0 1 0 1	ENQ	NAK	%	5	E	U	e	u	
0 1 1 0	ACK	SYN	&	6	F	V	f	v	
0 1 1 1	BEL	ETB	`	7	G	W	g	w	
1 0 0 0	BS	CAN	(8	H	X	h	x	
1 0 0 1	HT	EM)	9	I	Y	i	y	
1 0 1 0	LF	SUB	*	:	J	Z	j	z	
1 0 1 1	VT	ESC	+	;	K	[k	{	
1 1 0 0	FF	FS	,	<	L	\	l	 	
1 1 0 1	CR	GS	-	=	M]	m	}	
1 1 1 0	SO	RS	.	>	N	^	n	~	
1 1 1 1	SI	US	/	?	O		o	DEL	

Transmission Control

Format Control

Printable Character

Information Separator

Others

Byte-Stuffing

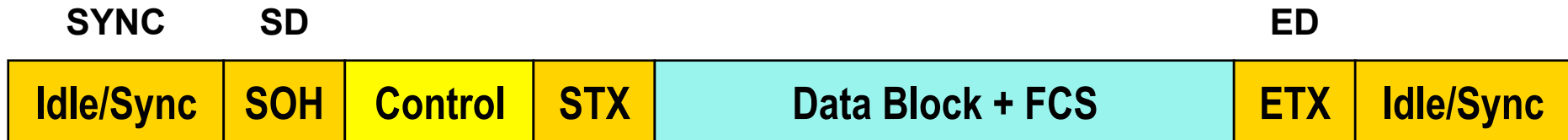
- **Some character-oriented protocols divide data stream into frames**
 - Old technique, not so important today
 - e.g. IBM BSC (Binary Synchronous Control) protocol
- **Data Link Escape (DLE) character indicates special meaning of next character**

Data to send:

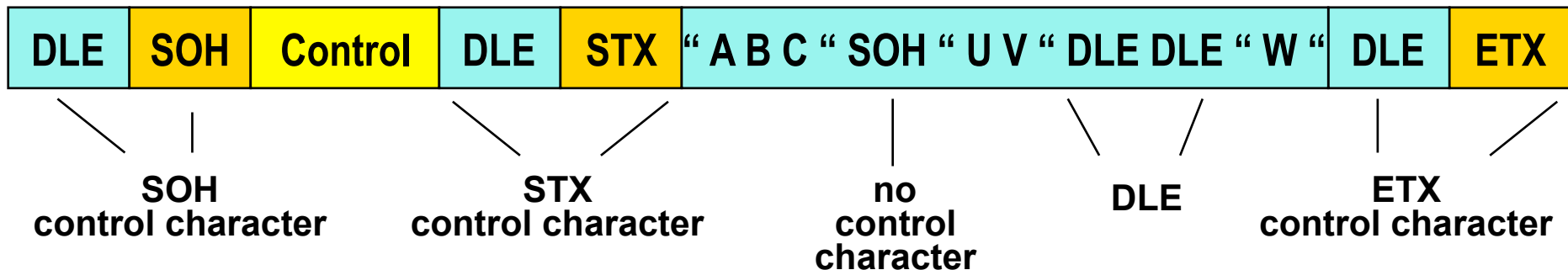
A B C DLE E F G ETX H I STX H



Character Based Transmission With And Without Protocol Transparence



Transmission in non-data transparent mode; control character *not* allowed in data block



Transmission in data-transparent mode with byte-stuffing;
control character allowed in data block

Byte-stuffing: DLE inside data portion will be doubled by sender;
receiver deletes this doubled DLE

Bit-Stuffing

- **Used in bit-oriented protocols**
 - Used by most protocols
 - Bits represent smallest transmission unit
- **HDLC-like framing: 01111110-pattern**
- **Rule:**
 - Transmitter-HW inserts a zero after five ones
 - Receiver rejects each zero after five ones

Data to send:

0100111111000111111100101100110

01111110

010011111100011111101100101100110

01111110

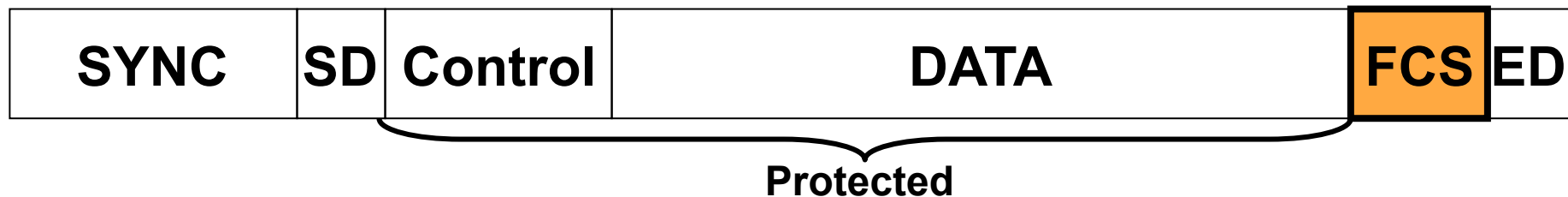
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Error Control

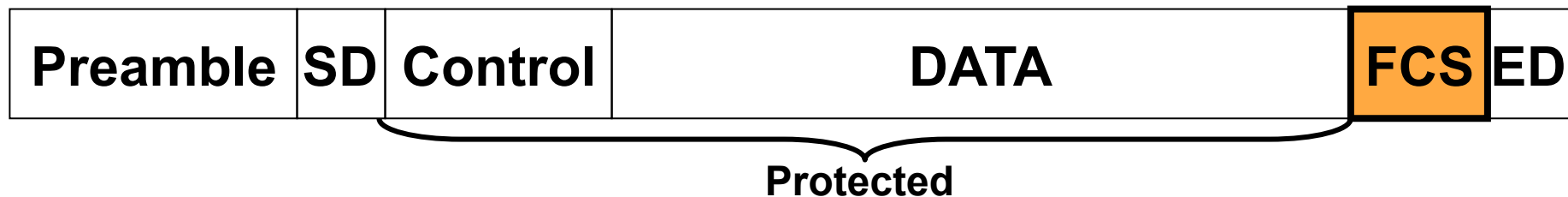
- **Focus on error detection**

- Include enough redundant information with each block of data to enable receiver to detect only errors occurred -> error detecting codes -> Frame Check Sequence
- After error detection a retransmission of frame is initiated through protocol feedback to the sender
 - Area of ARQ-techniques
 - Feedback Error Control



Frame Protection

- A frame check sequence (FCS) protects the **integrity** of our frame
 - From Sunspots, Mobile-Phones, Noise, Heisenberg and others
- **FCS is calculated upon data bits**
 - Different methods based on mathematical efforts: Parity, Checksum, CRC
- **Receiver compares its own calculation with FCS**



FCS Methods

- **Parity**
 - Even (10011101**1**) or odd (10011101**0**) parity bits
 - Examples: Asynchronous character-transmission and memory protection
- **Checksum**
 - Module 2 sum without carry bit (XOR operation)
 - Many variations and improvements
 - Examples: TCP and IP Checksums

Checksum Example: ISBN

- **100% Protection against**
 - Single incorrect digits
 - Permutation of two digits
- **Method:**
 - 10 digits, 9 data + 1 checksum
 - Each digit weighted with factors 1-9
 - Checksum = Sum modulo 11
 - If checksum=10 then use "X"

ISBN 0-13-086388-2

$$0*1+1*2+3*3+0*4+8*5+6*6+3*7+8*8+8*9 = 244$$
$$244 \text{ modulo } 11 = 2$$

Cyclic Redundancy Check

- **CRC is one of the strongest methods**
- **Bases on polynomial-codes**
 - Protected bits are used as coefficients of polynomial
 - This polynomial is mod 2 divided by a generator-polynomial
 - The rest is the CRC-Checksum
 - Bit error burst with a maximal length of generator-polynomial are detected 100%
- **Several standardized generator-polynomials**
 - CRC-16: $x^{16}+x^{15}+x^2+1$
 - CRC-CCITT: $x^{16}+x^{12}+x^5+1$

Error Control

- **Focus on error correction**
 - Include enough redundant information with to enable receiver to correct errors occurred -> error correcting codes ECC (important -> “Hamming Distance”)
 - Forward Error Control (FEC)
 - Required for "extreme" conditions
 - High BER (Bit Error Rate), EMR
 - Long delays, space links
 - Examples: Reed-Solomon codes, Hamming-codes

